EuroMPI/ASIA 2014

September 12th, 2014 Kyoto, Japan

# Distributed Behavioral Cartography of Timed Automata

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## Context: Formal Verification of Timed Systems (1/2)

- Need for early bug detection
  - Bugs discovered when final testing: expensive
  - $\rightsquigarrow$  Need for a thorough modeling and verification phase









## Context: Formal Verification of Timed Systems (2/2)

#### Use formal methods



A model of the system



#### A property to be satisfied

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### Context: Parameter Synthesis

- Timed systems are characterized by a set of timing constants
  - "The packet transmission lasts for 50 ms"
  - "The sensor reads the value every 10 s"
- Verification for one set of constants does not usually guarantee the correctness for other values
- Challenges
  - Numerous verifications: is the system correct for any value within [40; 60]?
  - Optimization: until what value can we increase 10?
  - **Robustness**: What happens if 50 is implemented with 49.99?

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#### Parameter synthesis

- Consider that timing constants are unknown constants (parameters)
- Find good values for the parameters

#### Outline

- 1 Behavioral Cartography of Timed Automata
- 2 Distributing the Cartography
- 3 A Master-Worker Scheme Using MPI
- **4** Implementation and Experiments
- 5 Conclusion and Perspectives

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Finite state automaton (sets of locations)



#### Finite state automaton (sets of locations and actions)



- Finite state automaton (sets of locations and actions) augmented with a set X of clocks [Alur and Dill, 1994]
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  - Transition guard: property to be verified to enable a transition
  - Clock reset: some of the clocks can be set to 0 at each transition







Examples of concrete runs



- Examples of concrete runs
  - Coffee with no sugar

























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■ Timed automaton (sets of locations, actions and clocks)



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  - "What are all possible parameter valuations such that one can get a coffee with 3 doses of sugar?"  $p_2 \le 8 \land p_2 \ge 3 \times p_1$

Partition the parameter state space into tiles

 Tile: constraint in which the discrete behavior ("same number of doses of sugar") is uniform



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## Behavioral Cartography: Partition

Application: given a linear-time property ("the coffee may have at least 3 doses of sugar"), one can partition the tiles into good and bad

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... but doing it efficiently is far from trivial in practice!

#### The general "shape" of the cartography is unknown in general



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ightarrow rules out the idea of partitioning the parameter space a priori

Calling the inverse method IM in parallel on two nodes starting from two close points will very probably yield the same tile  $\sim$  loss of efficiency



Idea: call the inverse method IM on points as far as possible

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Idea: call the inverse method IM on points as far as possible

But what does "as far as possible" mean for n nodes in m parameter dimensions?

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#### A Master-Worker Scheme

Traditional Master-Worker communication scheme

- Workers ask the master for a point, call IM on that point, and send the resulting tile to the master
- The master is responsible for the smart repartition of the data (*i.e.*, the points) between workers
  - In this work: 2 different algorithms for the master

## Sequential Algorithm

#### General idea

- **1** Enumerate all points starting from 0
- 2 When a point not yet covered by any tile is found, send it to the worker asking for work























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## Random+Sequential Algorithm

#### General idea

- **1** Try to find randomly a point not covered by any tile
- 2 After MAX consecutive failed attempts to find a point not covered by any tile, check sequentially all points starting from 0

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- **1** Try to find randomly a point not covered by any tile
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The second phase is costly, but necessary to ensure the full coverage of integer points

■ Otherwise, would only guarantee a coverage of, e.g., 99 %






















Master



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Master



... then switch to sequential enumeration to cover the remaining integer points

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### Implementation in a distributed version of IMITATOR

■ IMITATOR [A., Fribourg, Kühne, Soulat, 2012]

- "Inverse Method for Inferring Time AbstracT BehaviOR"
- 10,000 lines of OCaml code
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Distributed extension of IMITATOR using MPI

Using the OcamlMPI library

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- Distributed extension of IMITATOR using MPI
  - Using the OcamlMPI library
  - ... in which we found a bug!

# Description of the case studies

#### Sched3

- Parametric schedulability problem
- 2 parameters, 268 integer points

#### SIMOP

- Model of a networked automation system (NAS)
- 2 parameters, 10,201 integer points



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# Environment of the Experiments

#### Magi cluster (Paris 13)

- ∎ Intel Xeon X5570, 2.93 GHz, 6 cores/CPU, 2 CPUs/node
- Memory: 24 GB/node (2 GB/core)
- 40 Gb InfiniBand network

#### Software environment

- Linux 3.2.0, 64 bits
- gcc 4.7.2, ocamlc 3.12.1
- Bullx OpenMPI 1.8.2, OCamlMPI 1.01

### Graphical Comparison: Sched3



### Graphical Comparison: Sched3



### Graphical Comparison: Simop



### Graphical Comparison: Simop



# Analysis of the results: Sched3

Algorithm	Sequential	Random10	Random20
Time (seq)	40.29 s	N/A	N/A
# of cons. (seq)	59	N/A	N/A
Time (3 procs)	22.26 s	22.93 s	22.18 s
# of cons. (3 procs)	62	64	65
Time (36 procs)	5.08 s	3.48 s	3.70 s
<pre># of cons. (36 procs)</pre>	196	123	128

# Analysis of the results: Simop

Algorithm	Sequential	Random10	Random20
Time (seq)	121.91 s	N/A	N/A
# of cons. (seq)	48	N/A	N/A
Time (3 procs)	86.51 s	64.40 s	63.30 s
# of cons. (3 procs)	81	62	61
Time (36 procs)	35.23 s	17.87 s	18.51 s
<pre># of cons. (36 procs)</pre>	413	217	213

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# Interpretation of the experiments

#### Summary of the experiments

- Adding more workers always decreases the computation time
  - Decrease by a factor of 8 (resp. 12) with 36 nodes
- Random+sequential much more efficient than sequential, despite the 2nd phase cost
- Random+sequential more or less linear for Sched3, less for SIMOP

#### Limitations of the use cases

• Few tiles (48 for SIMOP, 59 for Sched3): Intrinsically limits the efficiency for many workers

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# Conclusion

#### First attempt to distribute the behavioral cartography

In fact first attempt for performing distributed parameter synthesis

#### Results quite promising

...although there is still a lot of space for improvement!

- Ongoing work: new algorithms
  - Master-worker with shuffle [completed]
  - Unsupervised workers with a common memory node [ongoing]
  - Totally decentralized [starting]

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  - Should we stop an ongoing execution of IM when its node was covered by another tile?



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#### Orthogonal problems

- Coverage of almost all the state space (e.g., 99%): towards a purely random algorithm?
- Parallel parametric verification using multi-core (based on,
  - e.g., [Evangelista et al., 2012])

# Bibliography

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# Additional explanation

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# Explanation for the 4 pictures in the beginning



Allusion to the Northeast blackout (USA, 2003) Computer bug Consequences: 11 fatalities, huge cost (Picture actually from the Sandy Hurricane, 2012)



Allusion to any plane crash (Picture actually from the happy-ending US Airways Flight 1549, 2009)



Allusion to the sinking of the Sleipner A offshore platform (Norway, 1991) No fatalities Computer bug: inaccurate finite element analysis modeling (Picture actually from the Deepwater Horizon Offshore Drilling Platform)



Allusion to the MIM-104 Patriot Missile Failure (Iraq, 1991) 28 fatalities, hundreds of injured Computer bug: software error (clock drift) (Picture of an actual MIM-104 Patriot Missile, though not the one of 1991)
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