

2018年9月8日星期六
北京，中國

Parametric timed automata: modeling and verifying real-time systems under uncertainty

Étienne André

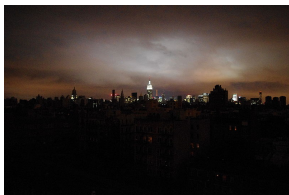
LIPN, Université Paris 13, CNRS, France

Feat. joint works with Giuseppe Lipari, and Sun Youcheng



Context: Verifying complex timed systems

- Real-time systems are everywhere
 - Hard **timing** constraints and **concurrency**
 - Criticality: risk for huge damages in case of unexpected behavior (**bug**)
 - Bugs discovered when final testing: **expensive**
- ↪ Need for a thorough specification and verification phase



Outline

- 1 Parametric timed automata
- 2 Modeling and verifying real-time systems with parameters
- 3 A case study: Verifying a real-time system under uncertainty
- 4 Conclusion and perspectives

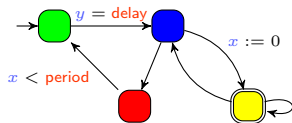
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Model checking timed concurrent systems

■ Use formal methods

[Baier and Katoen, 2008]



A **model** of the system

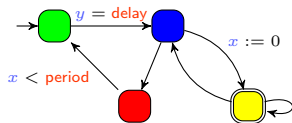
 is unreachable

A **property** to be satisfied

Model checking timed concurrent systems

■ Use formal methods

[Baier and Katoen, 2008]



A **model** of the system

?

$\models$

is unreachable

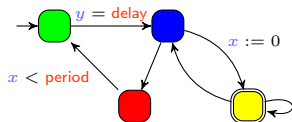
A **property** to be satisfied

■ Question: does the model of the system **satisfy** the property?

Model checking timed concurrent systems

■ Use formal methods

[Baier and Katoen, 2008]



?

$\equiv$

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A **model** of the system

A **property** to be satisfied

■ Question: does the model of the system **satisfy** the property?

Yes



No



Counterexample

Turing award (2007) to Edmund M. Clarke, Allen Emerson and Joseph Sifakis

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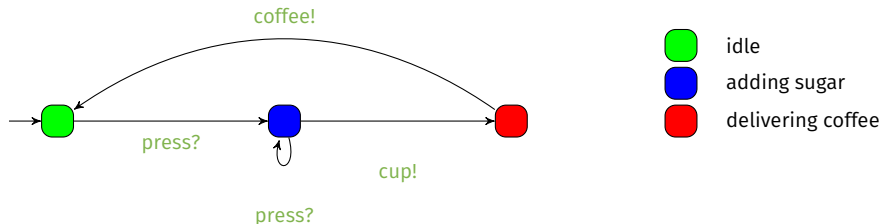
Timed automaton (TA)

- Finite state automaton (sets of locations)



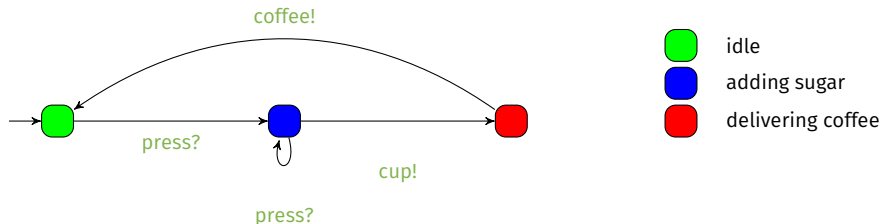
Timed automaton (TA)

- Finite state automaton (sets of locations and actions)



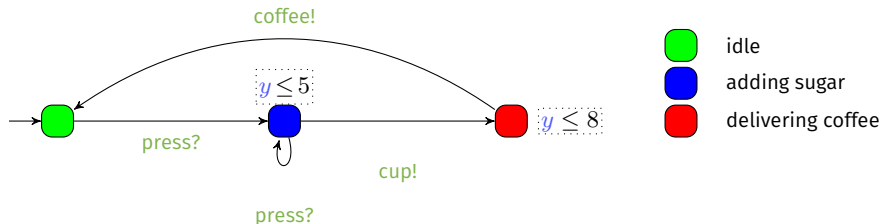
Timed automaton (TA)

- Finite state automaton (sets of **locations** and **actions**) augmented with a set X of **clocks** [Alur and Dill, 1994]
 - Real-valued variables evolving linearly **at the same rate**



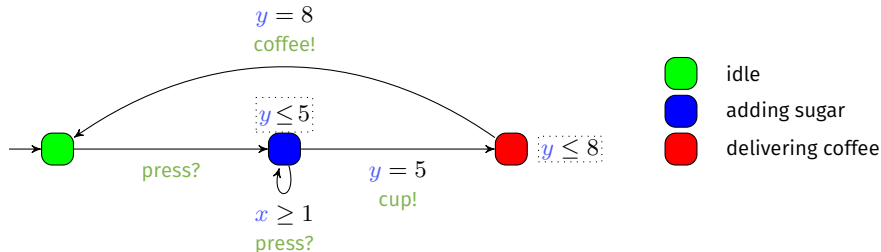
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 - Can be compared to integer constants in invariants
- Features
 - Location **invariant**: property to be verified to stay at a location



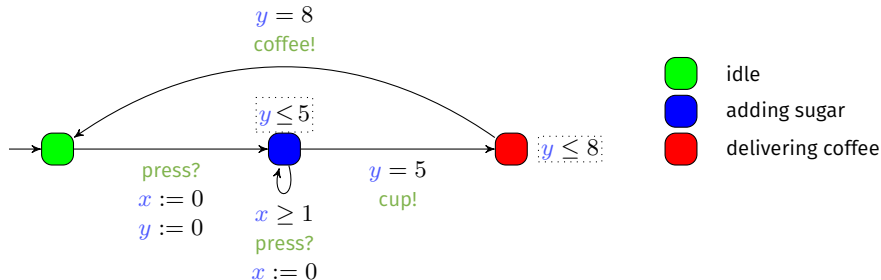
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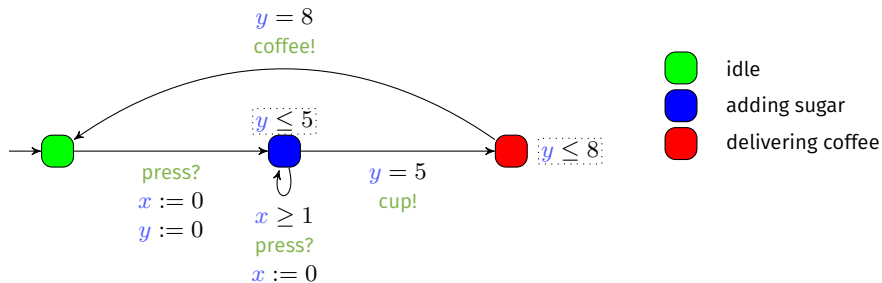


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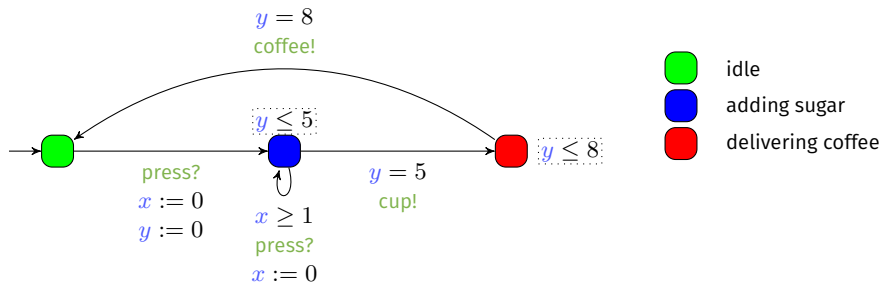
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- Features
 - Location **invariant**: property to be verified to stay at a location
 - Transition **guard**: property to be verified to enable a transition
 - Clock **reset**: some of the clocks can be **set to 0** along transitions



The most critical system: The coffee machine



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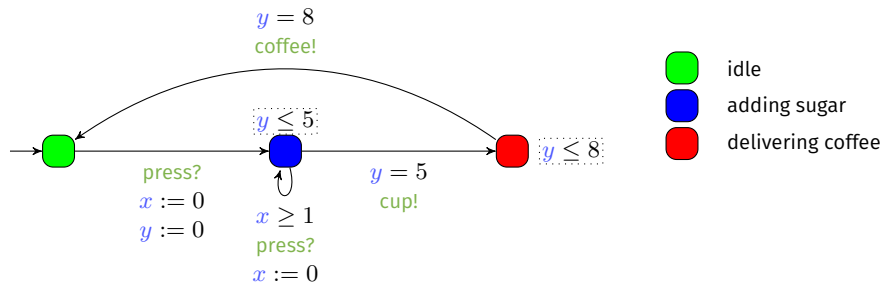


■ Example of concrete run for the coffee machine

■ Coffee with 2 doses of sugar

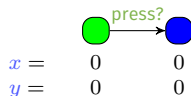

 $x = 0$
 $y = 0$

The most critical system: The coffee machine

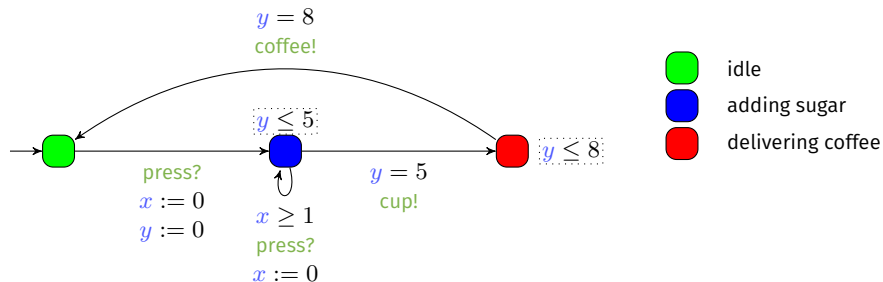


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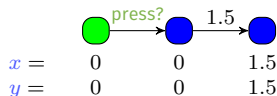


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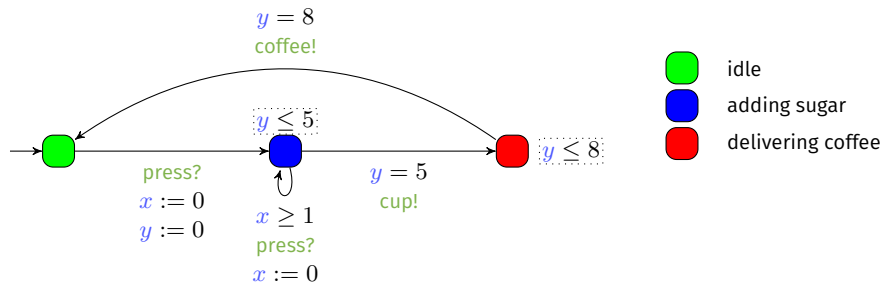


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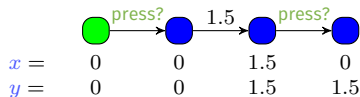


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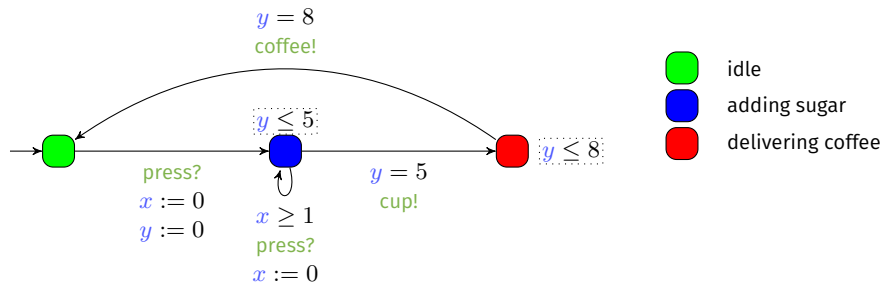


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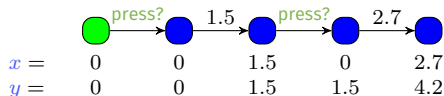


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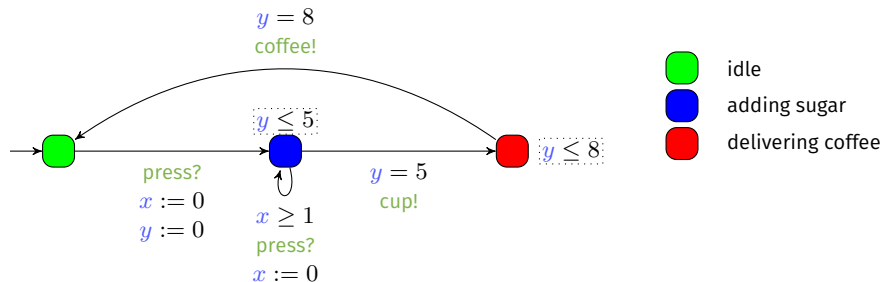


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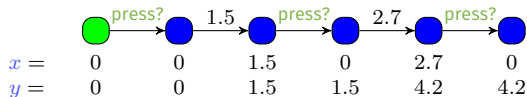


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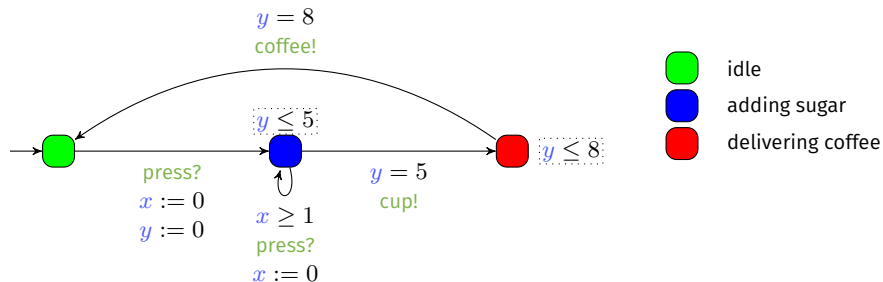


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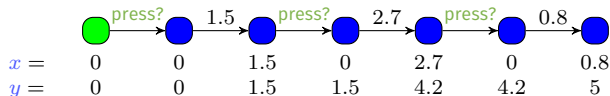


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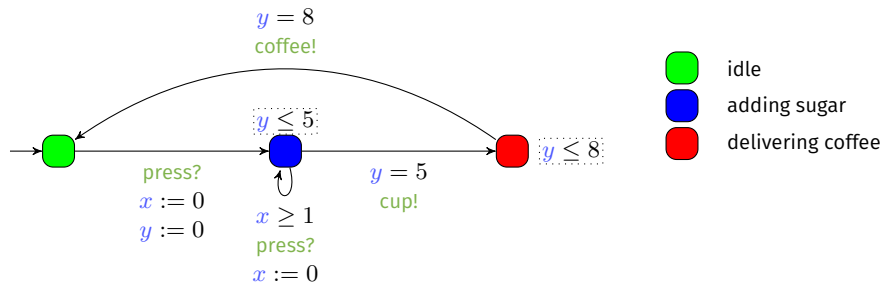


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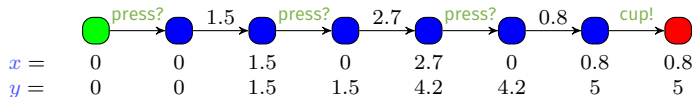


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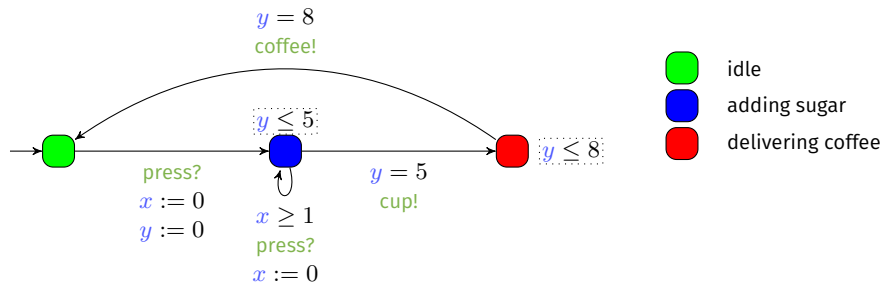


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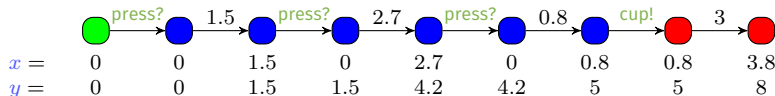


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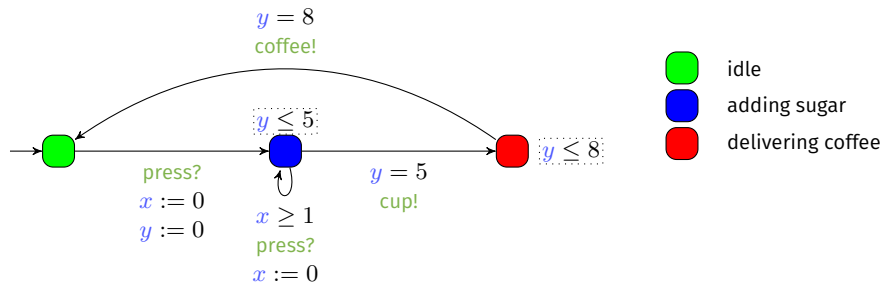


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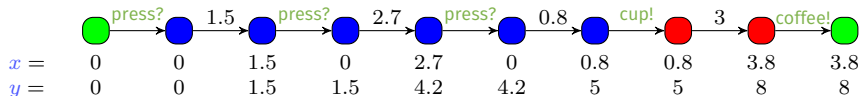


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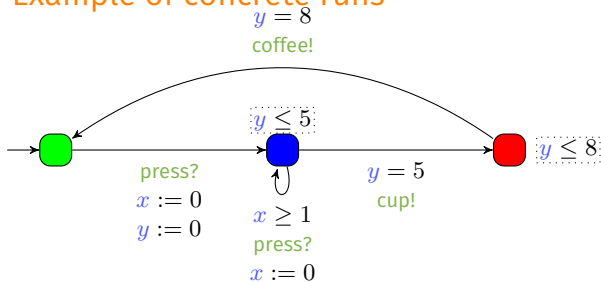
Concrete semantics of timed automata

- **Concrete state** of a TA: pair (l, w) , where
 - l is a **location**,
 - w is a **valuation** of each clock

Example: $(\blacksquare, (x=1.2, y=3.7))$

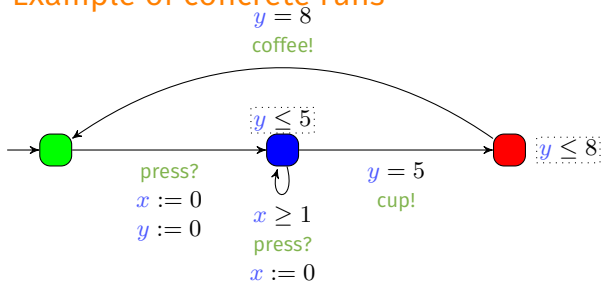
- **Concrete run**: alternating sequence of **concrete states** and **actions** or **time elapse**

Example of concrete runs



- Possible concrete runs for the coffee machine

Example of concrete runs



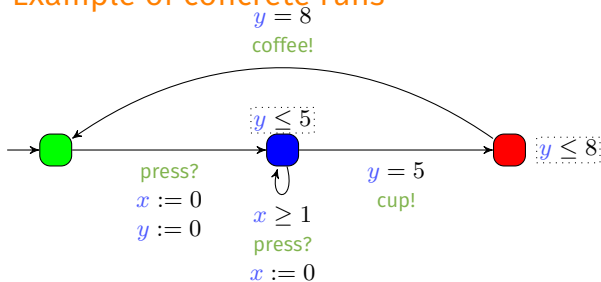
■ Possible concrete runs for the coffee machine

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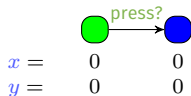
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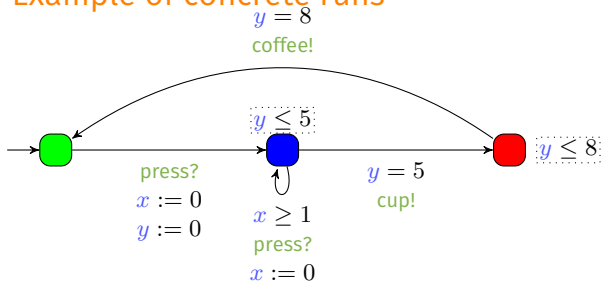


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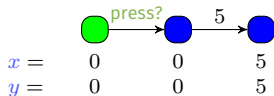


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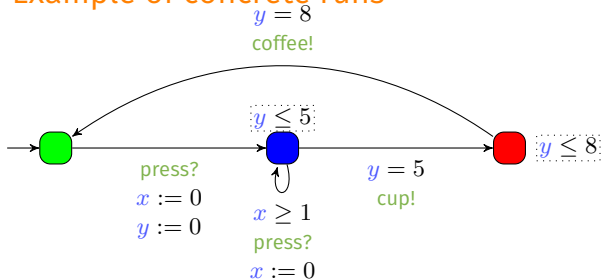


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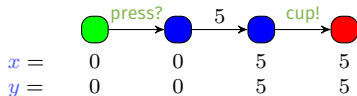


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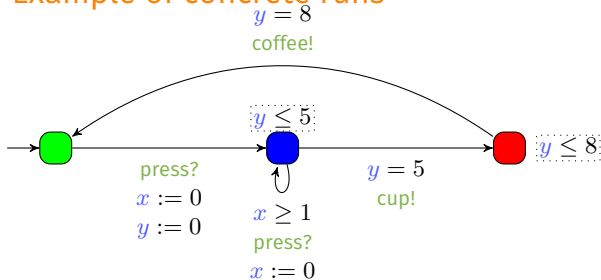


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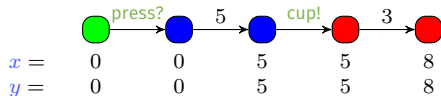


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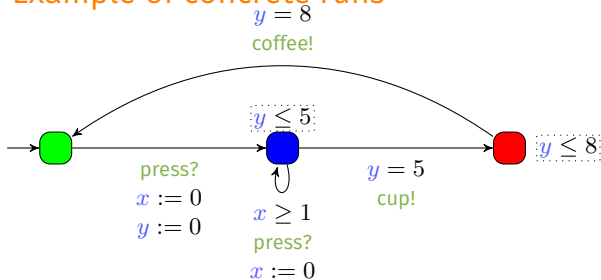


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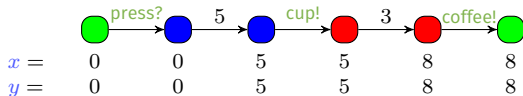


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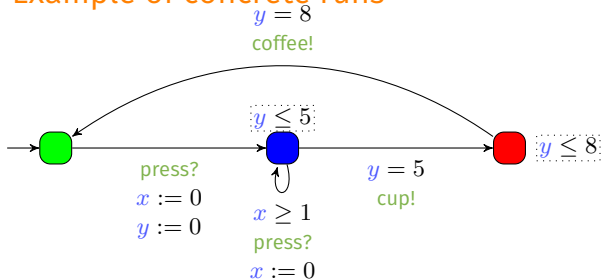


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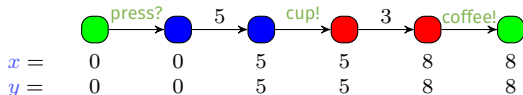


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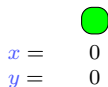


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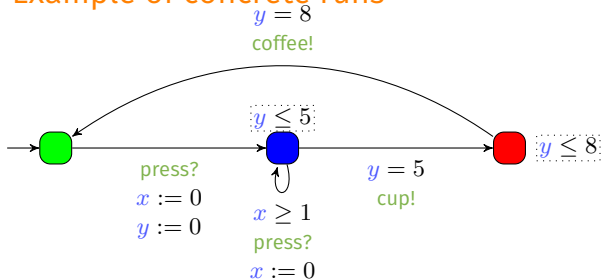
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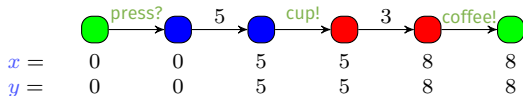


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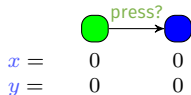


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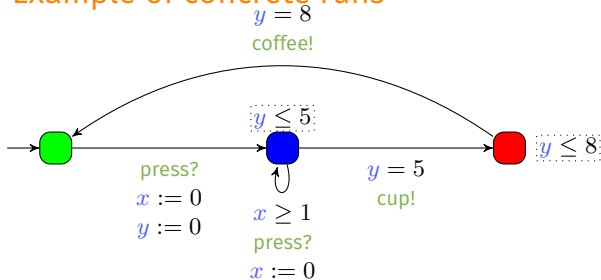
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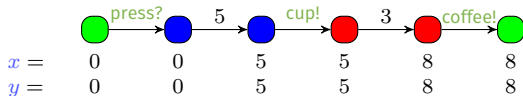


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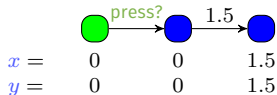


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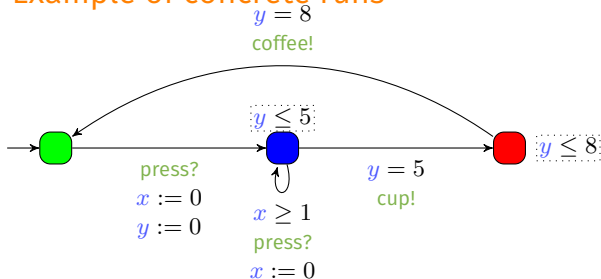
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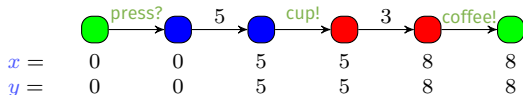


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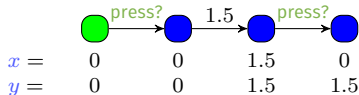


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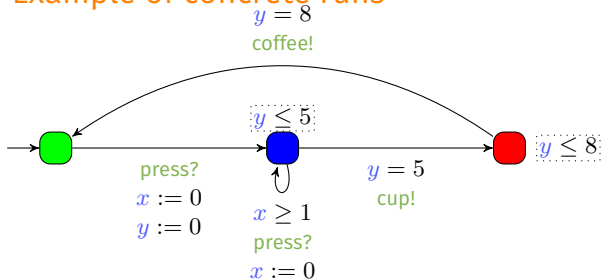
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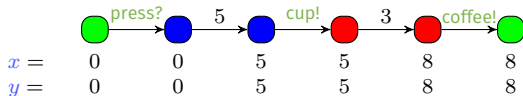


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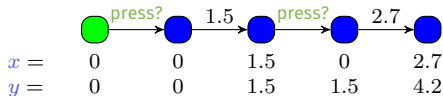


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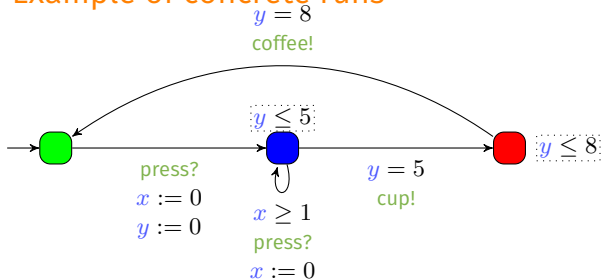
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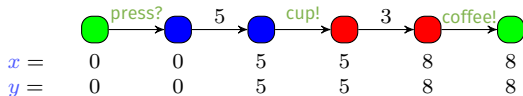


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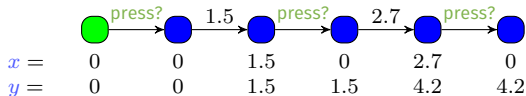


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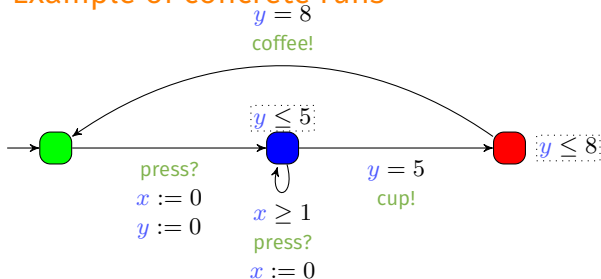
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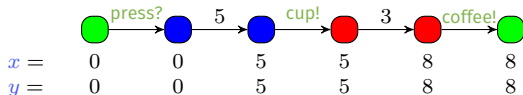


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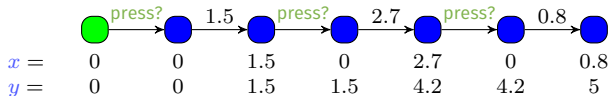


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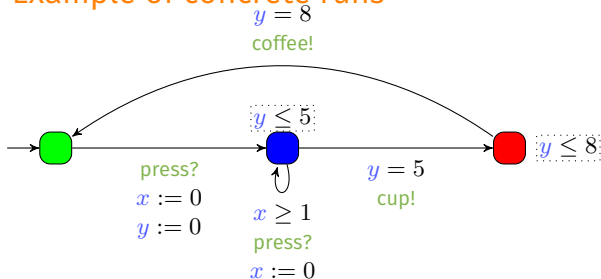
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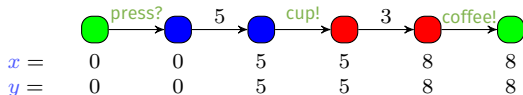


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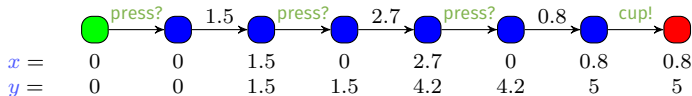


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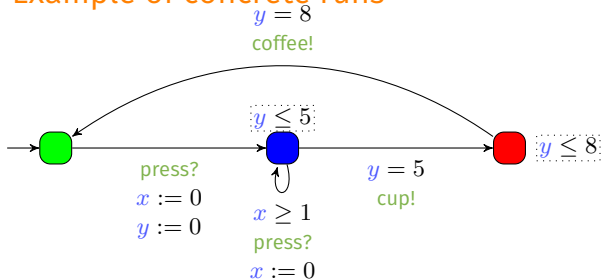
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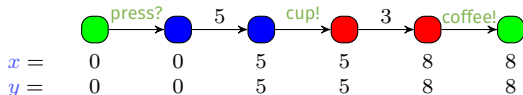


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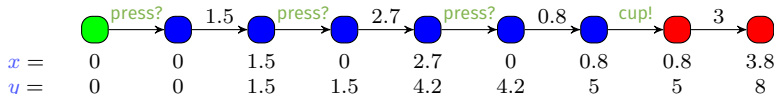


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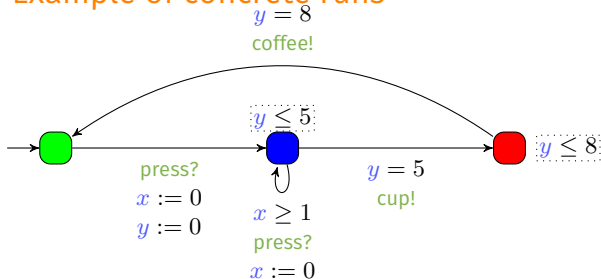
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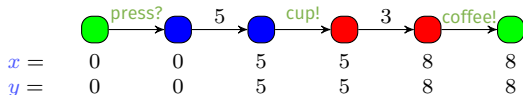


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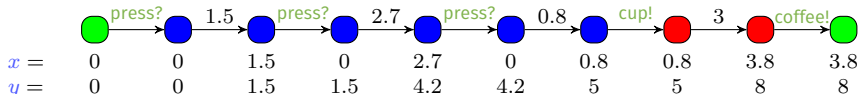
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$x =$
 $y =$

0	0	5	5	8	8
0	0	5	5	8	8

■ Coffee with 2 doses of sugar



$x =$
 $y =$

0	0	1.5	0	2.7	0	0.8	0.8	3.8	3.8
0	0	1.5	1.5	4.2	4.2	5	5	8	8

Timed automata: A success story

- An expressive formalism

- Dense time
- Concurrency

- A tractable verification in theory

- Reachability is PSPACE-complete

[Alur and Dill, 1994]

- A very efficient verification in practice

- Symbolic verification: relatively insensitive to constants
- Several model checkers, notably UPPAAL
- Long list of successful case studies

[Larsen et al., 1997]

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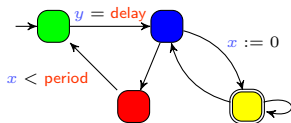
Beyond timed model checking: parameter synthesis

- Verification for **one** set of constants does not usually guarantee the correctness for other values
- Challenges
 - **Numerous verifications**: is the system correct for any value within $[40; 60]$?
 - **Optimization**: until what value can we increase 10?
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 - Consider that timing constants are unknown constants (**parameters**)

timed model checking



?

$\models$

 is unreachable

A **property** to be satisfied

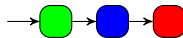
A **model** of the system

■ Question: does the model of the system satisfy the property?

Yes

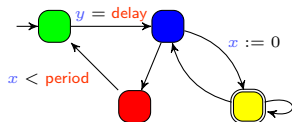


No



Counterexample

Parametric timed model checking



?

$\models$

 is unreachable

A **model** of the system

A **property** to be satisfied

- Question: **for what values of the parameters** does the model of the system **satisfy** the property?

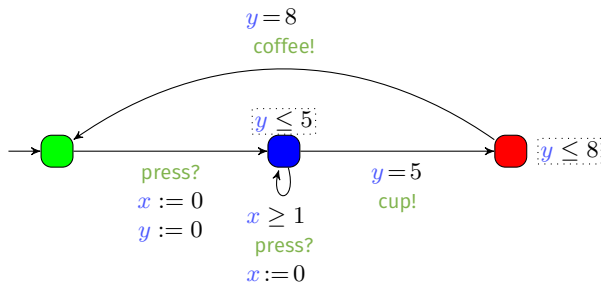
Yes if...



$$2\text{delay} > \text{period} \\ \wedge \text{period} < 20.46$$

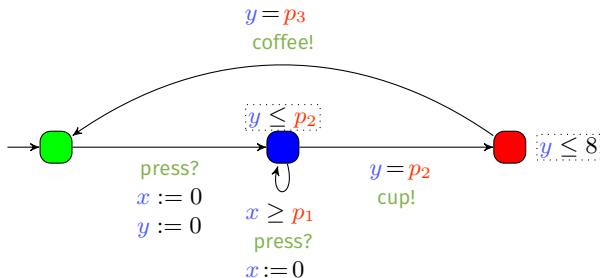
Parametric Timed Automaton (PTA)

- Timed automaton (sets of locations, actions and clocks)



Parametric Timed Automaton (PTA)

- Timed automaton (sets of locations, actions and clocks) augmented with a set P of parameters [Alur et al., 1993b]
 - Unknown constants compared to a clock in guards and invariants

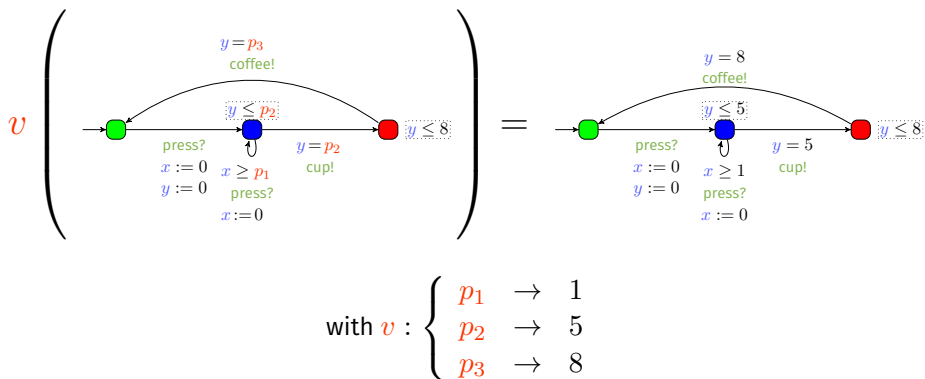


Notation: Valuation of a PTA

- Given a PTA $\mathcal{A}$ and a parameter valuation v , we denote by $v(\mathcal{A})$ the (non-parametric) timed automaton where each parameter p is valued by $v(p)$

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Symbolic semantics of parametric timed automata

- **Symbolic state** of a PTA: pair (l, C) , where
 - l is a **location**,
 - C is a convex polyhedron over X and P with a special form, called **parametric zone** [Hune et al., 2002]

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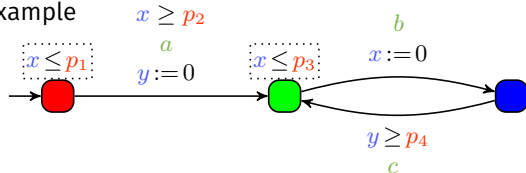
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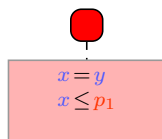
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■ Possible symbolic run for this PTA



Symbolic semantics of parametric timed automata

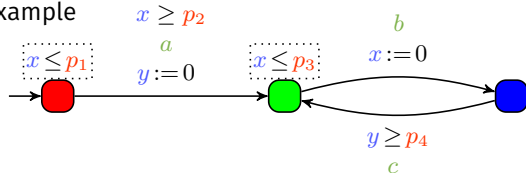
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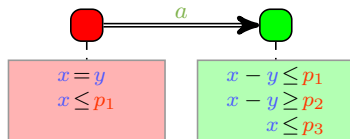
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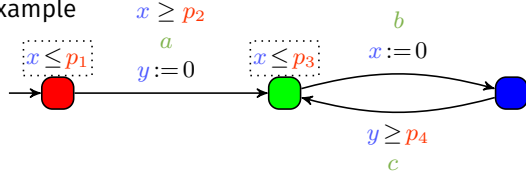
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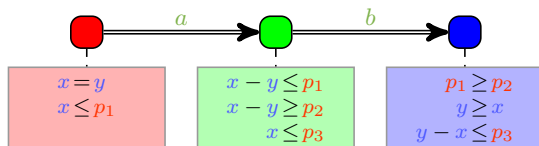
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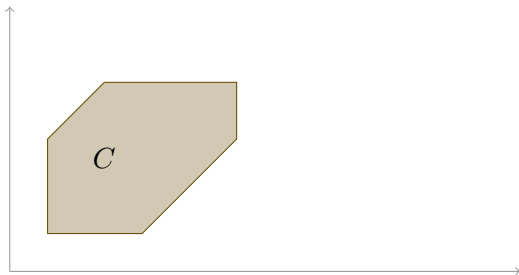


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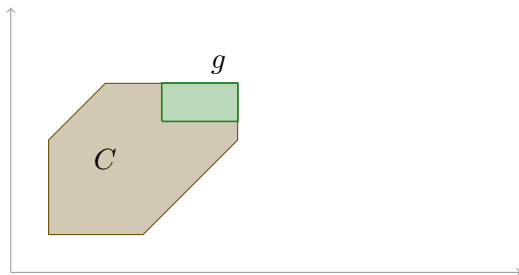
Symbolic semantics of PTA: Illustration

$$C' = [(C \cap g)]_{\textcolor{blue}{R}} \cap I(\textcolor{violet}{l}') \nearrow \cap I(\textcolor{violet}{l}')$$



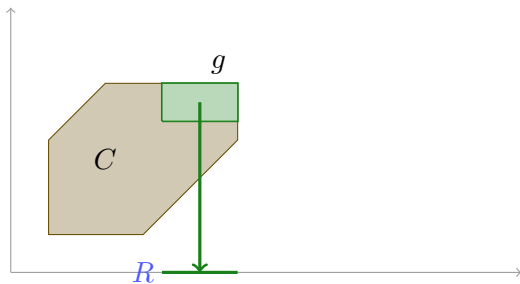
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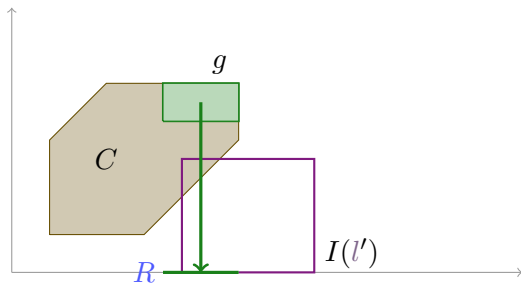
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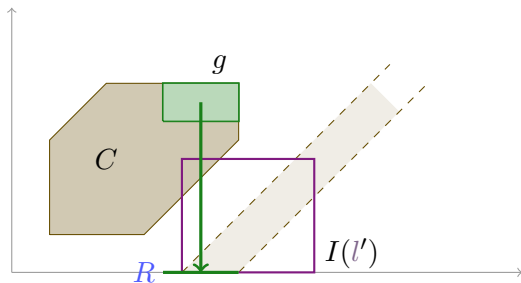
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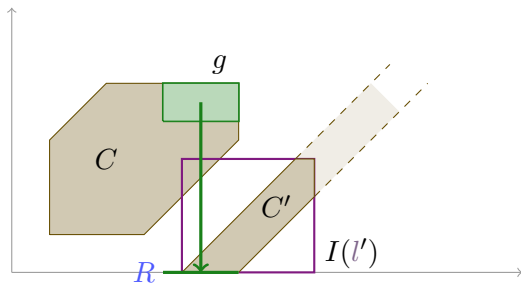
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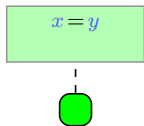
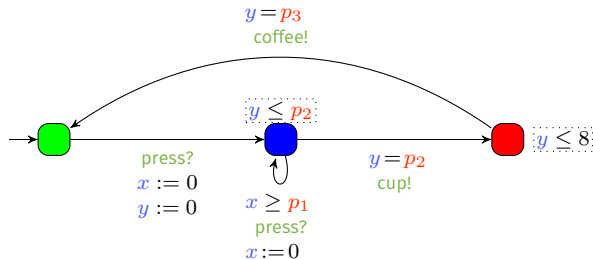


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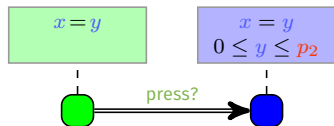
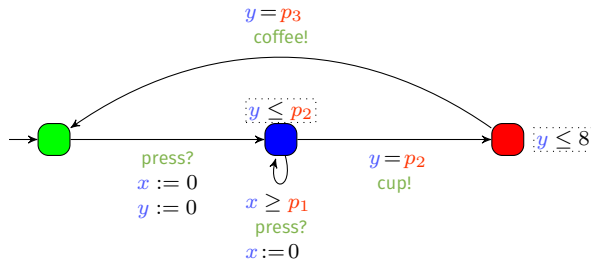
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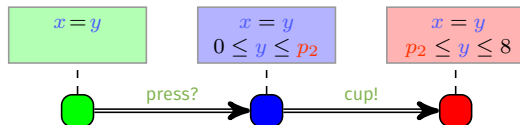
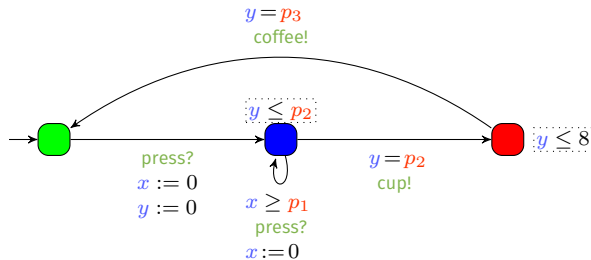
Symbolic exploration: Coffee machine



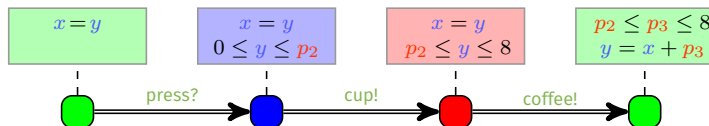
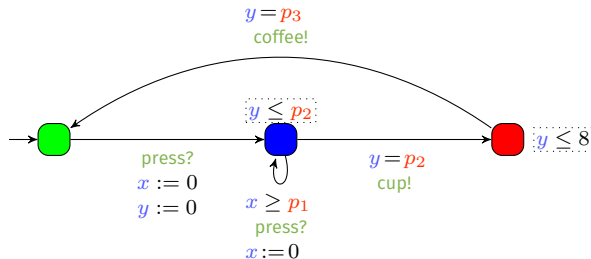
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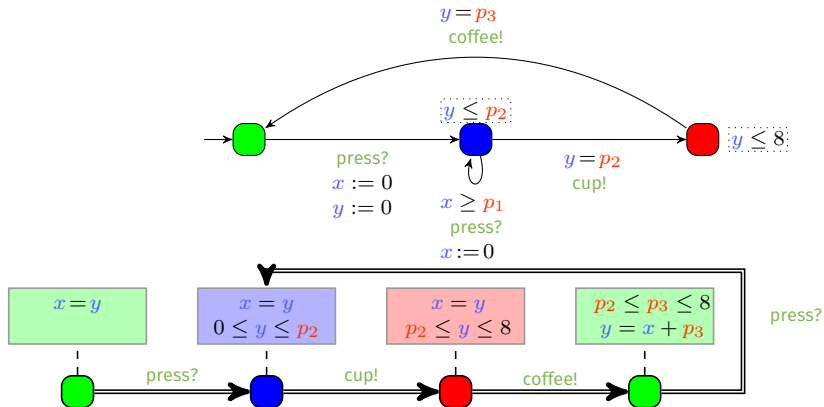
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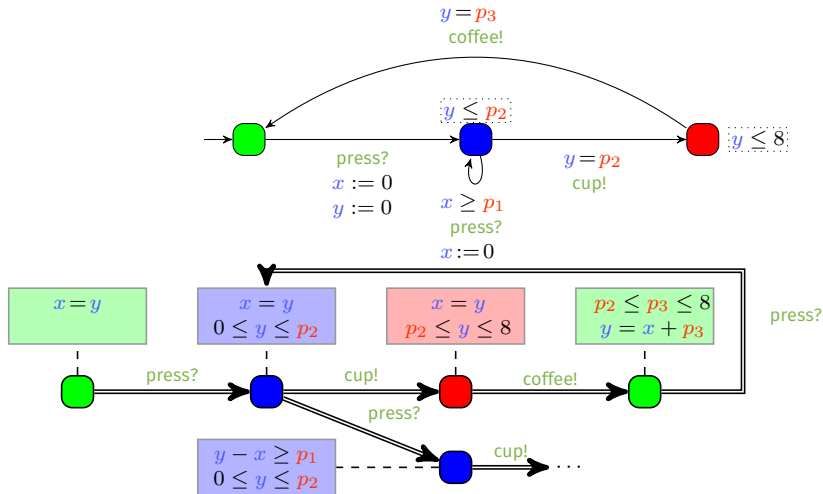
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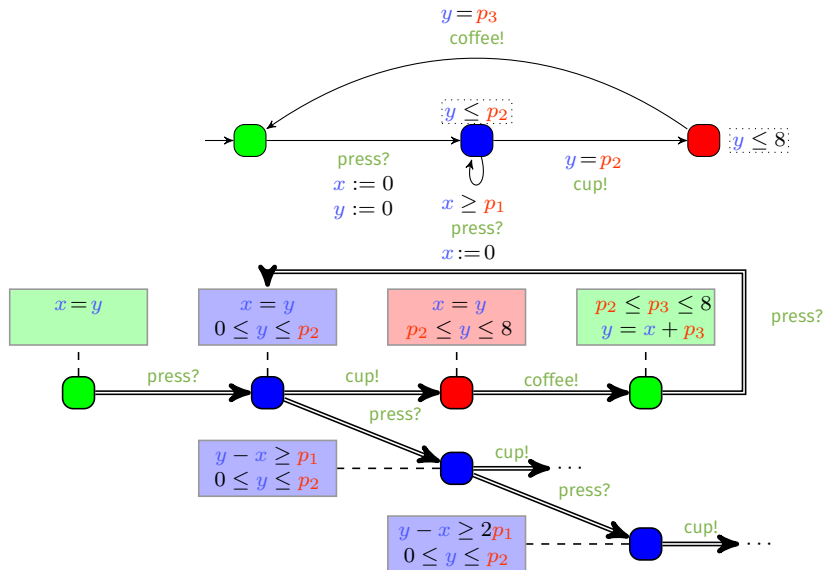
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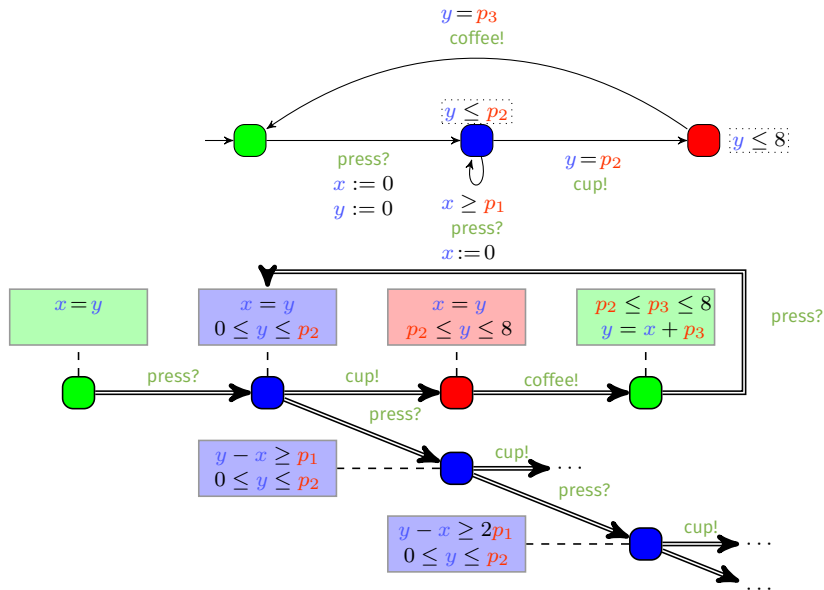
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If a decision problem is **undecidable**, it is hopeless to look for algorithms yielding exact solutions (because that is **impossible**)

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However, one can:

- design **semi-algorithms**: if the algorithm halts, then its result is correct
- design algorithms yielding over- or under-**approximations**

Decision and computation problems for PTA

- **EF-Emptiness** “Is the set of parameter valuations for which a given location l is reachable empty?”

Example: “Does there exist at least one parameter valuation for which I can get a coffee with 2 sugars?”

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Bad news

All interesting problems are undecidable for (general) parametric timed automata.

[ÉA, STTT 2017]

Outline

- 1 Parametric timed automata
- 2 Modeling and verifying real-time systems with parameters**
- 3 A case study: Verifying a real-time system under uncertainty
- 4 Conclusion and perspectives

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Context: Hard real-time embedded systems

- Modern hard real-time embedded systems are **distributed** in nature
- Many of them have **critical timing requirements**:
 - **automotive systems** (modern cars have 10-20 embedded boards connected by one or more CAN bus)
 - **avionics systems** (several distributed control boards connected by one or more dedicated networks)



- It is very important to check that **all tasks meet their deadlines**

Schedulability analysis

Real-time system:

- Set of tasks (with a period, a WCET and a **deadline**)
- One processor (uniprocessor) or more (multiprocessor)
- Scheduling policies: fixed priority (FPS), earliest deadline first (EDF)...

Definition (Schedulability analysis)

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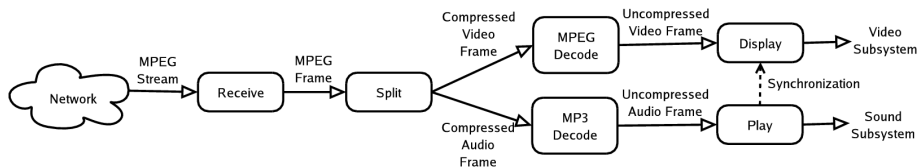
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In general, schedulability analysis is **hard**

Real-time pipelines

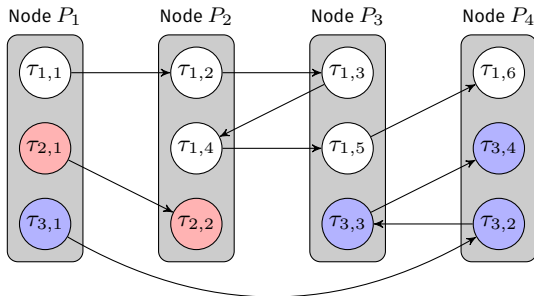
- Many real-time applications can be modeled as **pipelines** (also called **transactions**) of tasks



- Executed on a distributed (or multicore) system
- Activated cyclically (periodic or sporadic)
- Using **preemption**
 - Lower-priority tasks can be temporarily interrupted by a higher-priority task

Model

- A set of **pipelines** $\{\mathcal{P}^{(1)}, \dots, \mathcal{P}^{(p)}\}$ distributed over m **nodes**
- Each pipeline $\mathcal{P}^{(i)}$ is a chain of n_i **tasks** $\{\tau_{i,1}, \dots, \tau_{i,n_i}\}$
- Pipeline $\mathcal{P}^{(i)}$ has an end-to-end (**E2E**) deadline D_i and period T_i

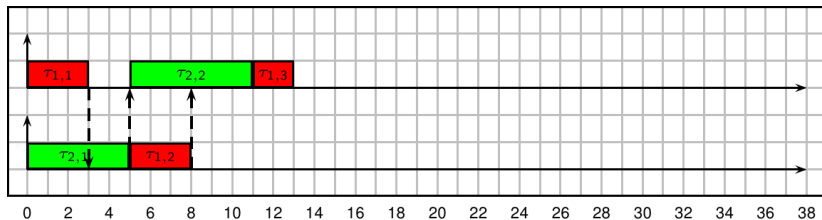
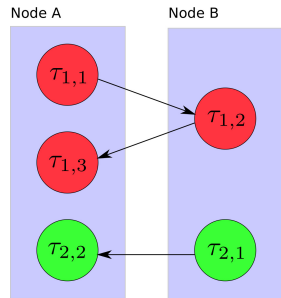


- **Scheduling Problem:** Guarantee that all pipelines complete before their E2E deadlines

Activations, jitter, deadline

■ An example

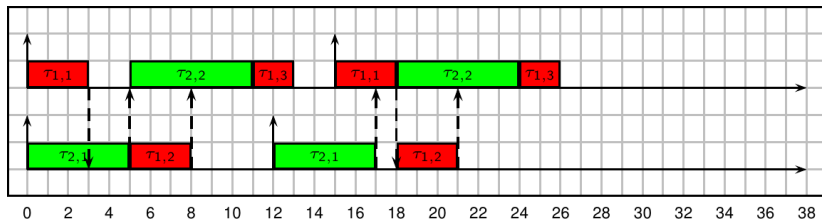
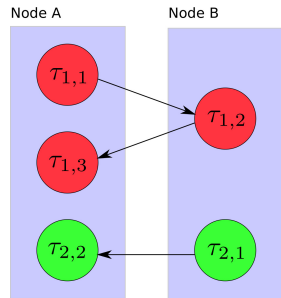
Task	Per.	E2E	Comp.	Resp.	Jitter	prio
$\tau_{1,1}$	15		3	3	0	HI
$\tau_{1,2}$	-		3	8	0-2	LO
$\tau_{1,3}$	-	15	2	13	3	LO
$\tau_{2,1}$	12		5	6	0	HI
$\tau_{2,2}$	-	12	6	?	0-1	ME



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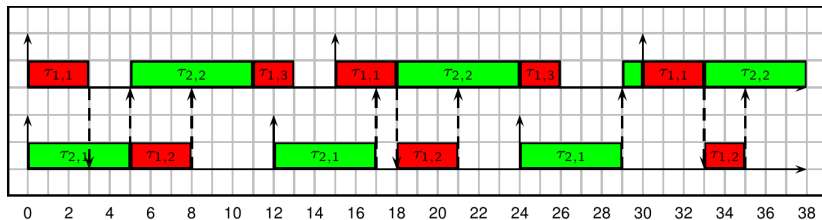
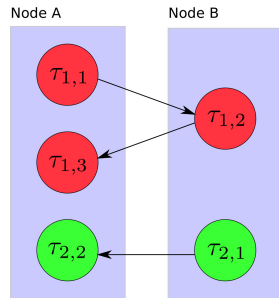
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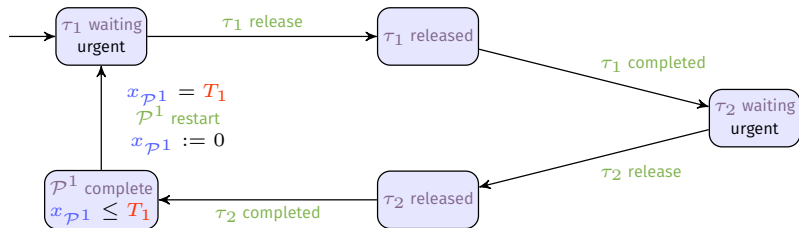
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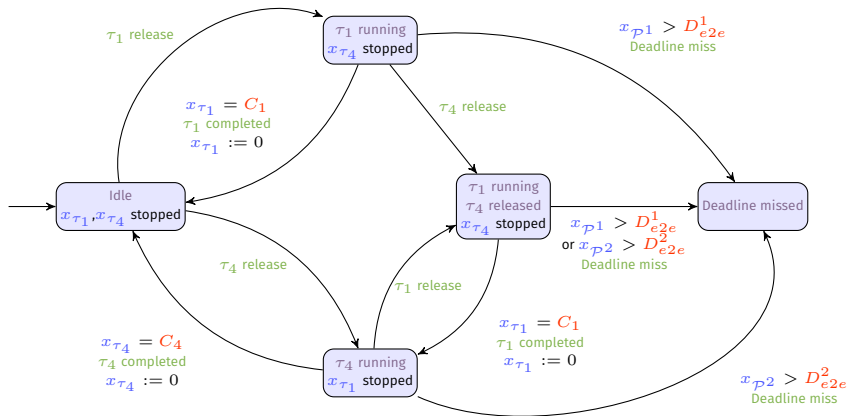
Enriching the model with parameters

- A task is identified by three parameters:
 - C_i is the **worst-case computation time** (or worst-case transmission time, in case it models a message)
 - R_i is the **task worst-case response time**, i. e., the worst case finishing time of any task instance relative to the activation of its pipeline.
 - J_i is the task **worst-case activation jitter**, i. e., the greatest time since its activation that a task must wait for all preceding tasks to complete their execution
- A parameter of major interest is the **computation time**

Modeling a task / pipeline



Modeling the fixed priority scheduler (preemptive)



Actually a PTA extended with **stopwatches** [Sun et al., 2013]
 an extension of stopwatch automata [Abbeddaïm and Maler, 2002]

Schedulability analysis with parametric model checking

Goal: parametric schedulability analysis

Given a real-time system and a scheduling policy, **synthesize** valuations (deadlines, periods...) such that the system is schedulable.

Modeling a real-time system with PTAs

- Each task or chain of task: one PTA
- Each scheduler: one PTA
- Use **stopwatches** to model preemption

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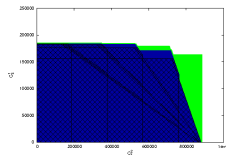
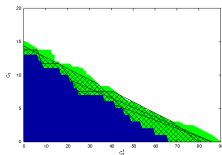
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Comparison with analytical methods

[Sun, Soulat, Lipari, André, Fribourg, FTSCS'13]

- Slower but much better in terms of completeness
- And can evaluate **robustness**



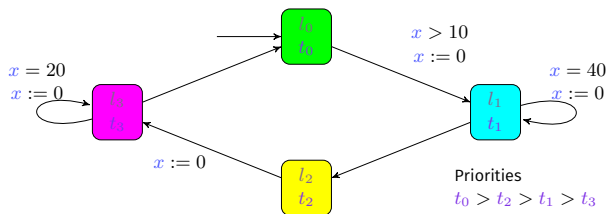
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A unified formalism: Parametric task automata

Extension of task automata [Norström et al., 1999, Fersman et al., 2007] with **parameters**

[André, FMICS'17]

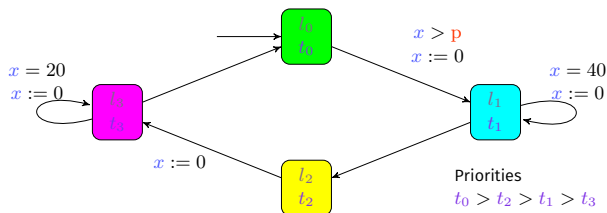


Task	B	W	D
t_0	0	1	2
t_1	4	4	20
t_2	0	1	4
t_3	2	2	10

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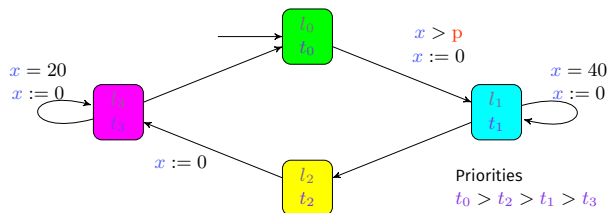


Task	B	W	D
t_0	0	1	2
t_1	4	4	20
t_2	0	1	p'
t_3	2	2	10

A unified formalism: Parametric task automata

Extension of task automata [Norström et al., 1999, Fersman et al., 2007] with **parameters**

[André, FMICS'17]



Task	B	W	D
t_0	0	1	2
t_1	4	4	20
t_2	0	1	p'
t_3	2	2	10

Parametric task automata can model

- Preemption
- Periodic tasks, sporadic tasks, pseudo-periodic tasks...
- Dependencies between tasks
- Offset, jitter
- **Uncertainty**
- **Uniprocessor only**

Parametric task automata: theory and practice

Schedulability-emptiness (“is the set of valuations for which the system is schedulable empty?”)

- Undecidable in general
- Decidable under some assumptions

[André, FMICS'17]

Parametric task automata: theory and practice

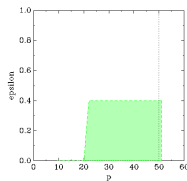
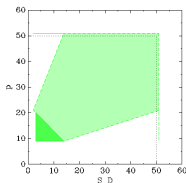
Schedulability-emptiness (“is the set of valuations for which the system is schedulable empty?”)

- Undecidable in general
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[André, FMICS'17]

Implementation in IMITATOR

- Translation into a network of parametric stopwatch automata
- Schedulability analysis
- Parametric and/or robust schedulability analysis



Outline

- 1 Parametric timed automata
- 2 Modeling and verifying real-time systems with parameters
 - Real-time systems
 - Modeling real-time systems under uncertainty
 - Parametric task automata
 - **Verification**
 - IMITATOR in a nutshell
- 3 A case study: Verifying a real-time system under uncertainty
- 4 Conclusion and perspectives

Parametric verification of real-time systems

Many problems can be reduced to parametric reachability (EFsynth): **find parameter valuations for which a given state is (un)reachable**

☹️ This problem is undecidable for PTAs and many subclasses

[ÉA, STTT 2017]

😊 But we can still compute part (and often all) of the solution

Interesting problems:

- Find parameter valuations for which no deadline violation occurs (i. e., for which the system is **schedulable**)
- Compute the worst-case computation time
- Find the parametric WCET when the jitter is unknown

Parametric model checking applied to schedulability analysis

Advantages: **Very expressive** (in fact Turing-complete)

- 😊 Periodic tasks, sporadic tasks...
- 😊 Task dependencies
- 😊 Data transmission
- 😊 Jitters, offsets
- 😊 Uncertainty
- 😊 All possible schedulers

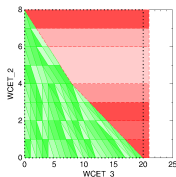
Drawback: **slow** (intractable for very large systems)

- 😞 limited to small or medium-sized systems

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- A tool for modeling and verifying **timed concurrent systems** with unknown constants modeled with **parametric timed automata**
 - Communication through (strong) broadcast synchronization
 - Rational-valued shared discrete variables
 - **Stopwatches**, to model schedulability problems with preemption
- Synthesis algorithms
 - (non-Zeno) parametric model checking (using a subset of **TCTL**)
 - Language and trace preservation, and robustness analysis
 - Parametric deadlock-freeness checking



IMITATOR

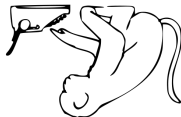
Under continuous development since 2008

[André et al., FM'12]

A library of benchmarks

- Communication protocols
- Schedulability problems
- Asynchronous circuits
- ...and more

Free and open source software: Available under the GNU-GPL license



IMITATOR

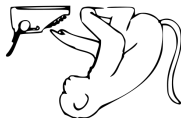
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Try it!

www.imitator.fr

Some success stories

- Modeled and verified an **asynchronous memory circuit** by ST-Microelectronics
- Parametric schedulability analysis of a prospective architecture for the flight control system of the **next generation of spacecrafts** designed at ASTRIUM Space Transportation [Fribourg et al., 2012]
- Verification of software product lines [Luthmann et al., 2017]
- Offline monitoring [ÉA, Hasuo, Waga @ ICECCS'18]
- Formal timing analysis of **music scores** [Fanchon and Jacquemard, 2013]
- Solution to a challenge related to a **distributed video processing system** by Thales

Outline

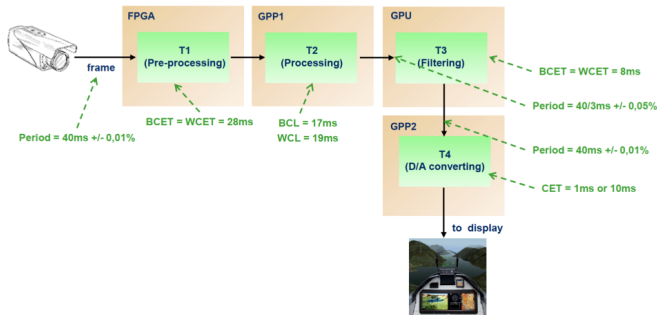
- 1 Parametric timed automata
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The FMTV 2015 Challenge (1/2)

Challenge by Thales proposed during the WATERS 2014 workshop
Solutions presented at WATERS 2015

System: an unmanned aerial video system with **uncertain periods**

- Period constant but with a small uncertainty (typically 0.01 %)
- Not a jitter!



The FMTV 2015 Challenge (2/2)

Goal

Compute the end-to-end BCET and WCET times for a buffer size of $n = 1$ and $n = 3$

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☹ Not a typical parameter synthesis problem?

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The FMTV 2015 Challenge (2/2)

Goal

Compute the end-to-end BCET and WCET times for a buffer size of $n = 1$ and $n = 3$

☹ Not a typical parameter synthesis problem?

- No parameters in the specification

😊 A typical parameter synthesis problem

- The end-to-end time can be set as a **parameter**... to be synthesized
- The uncertain period is typically a **parameter** (with some constraint, e.g., $P1 \in [40 - 0.004, 40 + 0.004]$)

Methodology

- 1 Propose a PTA model with **parameters** for uncertain periods and the end-to-end time

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Note: not eliminating parameters allows one to know for **which values of the periods** the best / worst case execution times are obtained.

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- 5 Eliminate all parameters but the end-to-end time
- 6 Exhibit the minimum and the maximum

Note: not eliminating parameters allows one to know for **which values of the periods** the best / worst case execution times are obtained.

To build the PTA model

■ Uncertainties in the system:

- $P1 \in [40 - 0.004, 40 + 0.004]$
- $P3 \in [\frac{40}{3} - \frac{1}{150}, \frac{40}{3} + \frac{1}{150}]$
- $P4 \in [40 - 0.004, 40 + 0.004]$

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■ Parameters:

- P1_uncertain
- P3_uncertain
- P4_uncertain

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■ Parameters:

- P1_uncertain
- P3_uncertain
- P4_uncertain

■ The end-to-end latency (another parameter): E2E

■ Others:

- the register between task 2 and task 3: discrete variable $\text{reg}_{2,3}$
- the buffer between task 3 and task 4: $n = 1$ or $n = 3$

Simplification

- T1 and T2 are synchronised; T1, T3 and T4 are asynchronised
 - (exact modeling of the system behaviour is too heavy)

Simplification

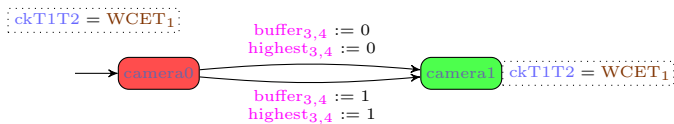
- T1 and T2 are synchronised; T1, T3 and T4 are asynchronised
 - (exact modeling of the system behaviour is too heavy)
- We choose a single arbitrary frame, called the **target** one
- We assume the system is initially in an arbitrary status
 - This is our only uncertain assumption (in other words, can the periods deviate from each other so as to yield any arbitrary deviation?)

The initialization automaton

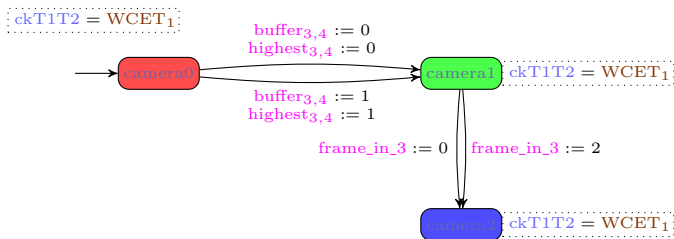
$$\text{ckT1T2} = \text{WCET}_1$$



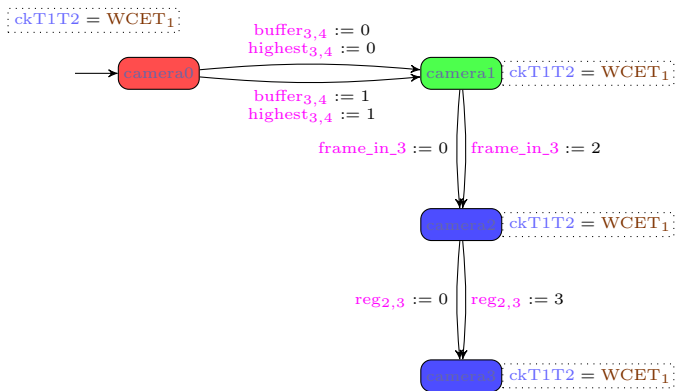
The initialization automaton



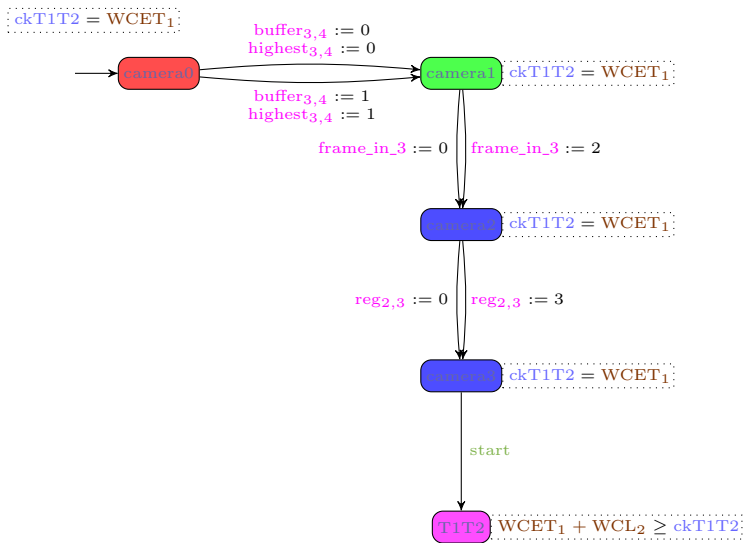
The initialization automaton



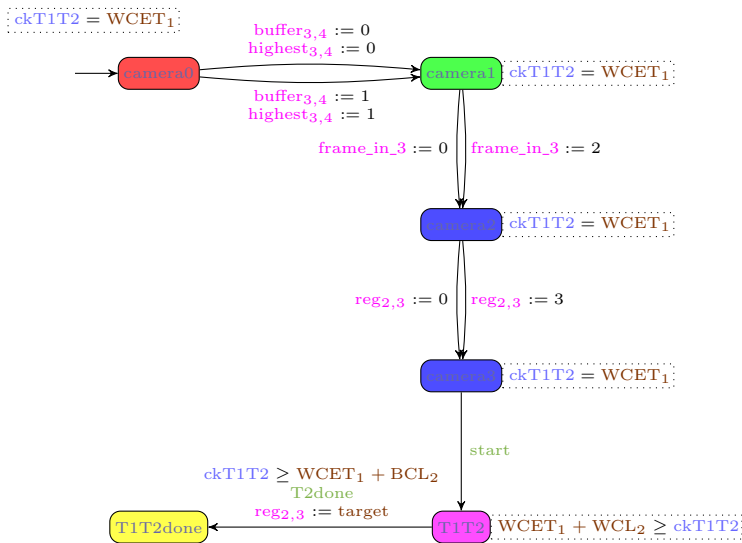
The initialization automaton



The initialization automaton



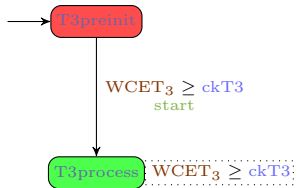
The initialization automaton



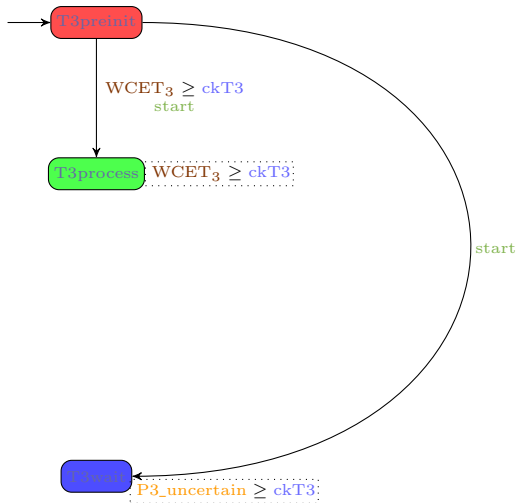
Task T3



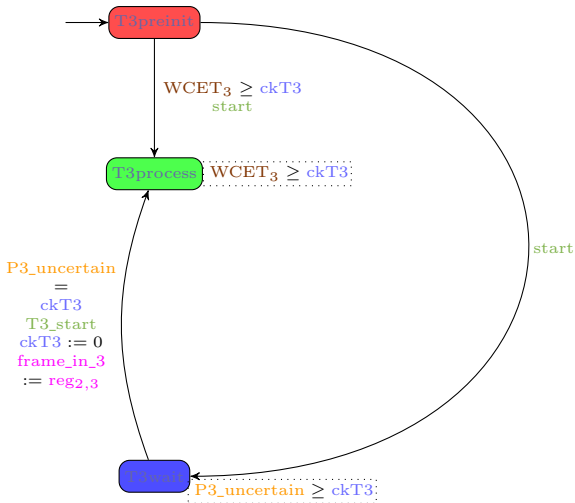
Task T₃



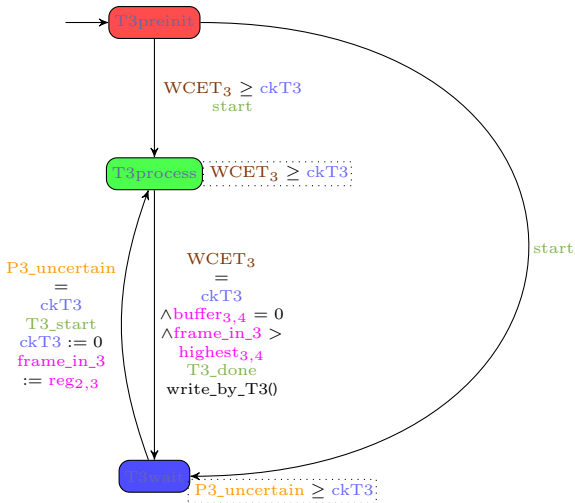
Task T3



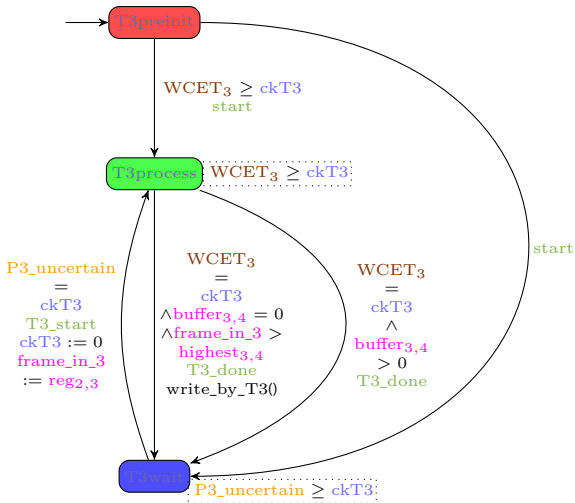
Task T3



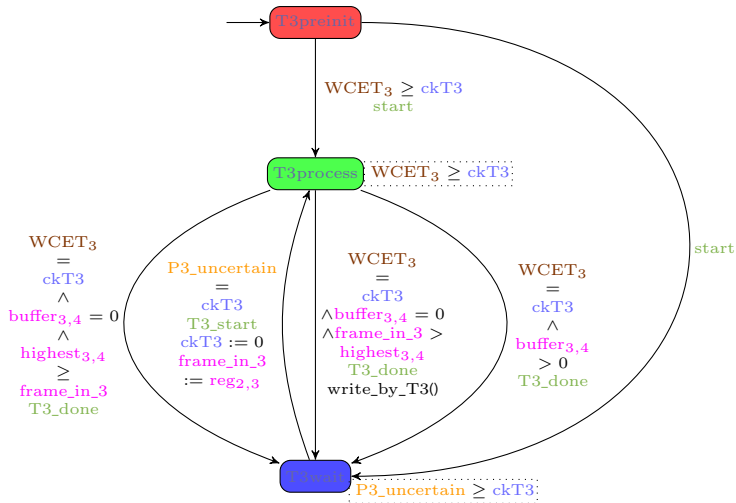
Task T3



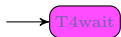
Task T3



Task T3



Task T₄



$P4_uncertain \geq ckT4$

Task T4

$P4_uncertain = ckT4$
 $\wedge buffer_{3,4} > 0$
 $ckT4 := 0$
 $read_by_T4()$

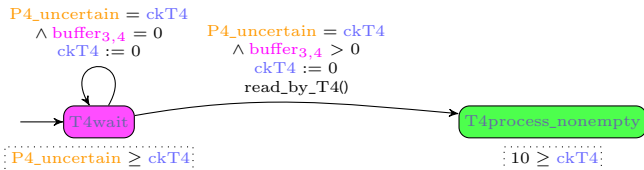
→ T4wait

$P4_uncertain \geq ckT4$

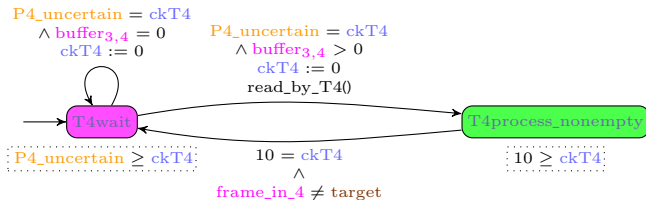
T4process_nonempty

$10 \geq ckT4$

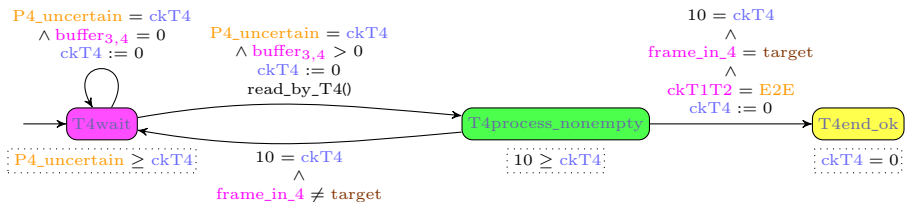
Task T4



Task T4



Task T4



Results

E2E latency results for $n = 1$ and $n = 3$

	$n = 1$	$n = 3$
min E2E	63 ms	63 ms
max E2E	145.008 ms	225.016 ms

Results obtained using IMITATOR in a few seconds

[ÉA, Lipari, Sun @ WATERS'15]

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Summary

■ Finite-state automata

- 😊 Mostly decidable results
- 😊 Efficient model checking algorithms
- 😞 Miss the quantitative aspects
- 😊 Many powerful tools

■ Timed automata

- 😊 Finite abstract semantics
- 😊 Some decidable results
- 😞 Some undecidable results
- 😊 Several powerful tools

■ Parametric timed automata

- 😊 Very expressive
- 😞 No finite abstract semantics
- 😞 Almost only undecidability results
- 😊 Some powerful tools

Perspectives

Address harder problems

- Thales challenge: what is the **minimum time between two lost frames?** (due to the uncertain periods)
 - Requires to model check **thousands of frame processings**

Improve the efficiency of parameter synthesis techniques

- Distributed parameter synthesis
 - Distribution over a cluster [ÉA, Coti, Nguyen @ ICFEM 2015]
 - Multi-core synthesis [Laarman et al., 2013]
 - Distributed synthesis based on locations [Zhang et al., 2016]
- Machine learning [Li et al., 2017]

Beyond (parametric) timed automata

Beyond time...

- Cost, temperature, energy

- Hybrid automata

[Alur et al., 1993a, Alur et al., 1995]

- Very expressive, but often undecidable

- Some interesting software (including **SpaceEx** [Frehse et al., 2011])

Probabilities

- Useful when a property cannot be proved with full certainty

- Communication protocols, failures...

- Another way to model systems known with limited precision

Security

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Best paper award.



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Additional explanation

Explanation for the 4 pictures in the beginning



Allusion to the Northeast blackout (USA, 2003)
Computer bug
Consequences: 11 fatalities, huge cost
(Picture actually from the Sandy Hurricane, 2012)



Error screen on the earliest versions of Macintosh



Allusion to the sinking of the Sleipner A offshore platform (Norway, 1991)
No fatalities
Computer bug: inaccurate finite element analysis modeling
(Picture actually from the Deepwater Horizon Offshore Drilling Platform)



Allusion to the MIM-104 Patriot Missile Failure (Iraq, 1991)
28 fatalities, hundreds of injured
Computer bug: software error (clock drift)
(Picture of an actual MIM-104 Patriot Missile, though not the one of 1991)

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Source of the graphics used II



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Title: Smiley green alien big eyes (cry)

Author: LadyofHats

Source: https://commons.wikimedia.org/wiki/File:Smiley_green_alien_big_eyes.svg

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