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Monitoring cyber-physical systems under uncertainty

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Motivation: automotive industry

- Modern cars embed several processors and produce logs



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start    2.3
gear1    5.8
gear2    9.2
gear3    18.5
gear2    42.1
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 - “It never happens that gear1 and gear3 are separated by less than 5 s”

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⇒ Monitoring

Larger motivation: data collection and management

- Personal mobile devices collect large amounts of **data**



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These data can also come in the form of a timed log
start walking

2.3

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These data can also come in the form of a timed log

start walking

2.3

walk faster

6.3

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These data can also come in the form of a timed log

start walking	2.3
walk faster	6.3
receive SMS	15.8

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These data can also come in the form of a timed log

start walking	2.3
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receive SMS	15.8
read SMS	19.2

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sound of someone bumping into a lamp	22.5

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These data can also come in the form of a timed log

start walking	2.3
walk faster	6.3
receive SMS	15.8
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- Key challenge: manage these data
 - Verify properties: “has the owner bumped into a street lamp”
 - key applications (health, ...)
 - **Deduce** information:
 - “what are the minimum/maximum intervals without visiting this shop”?
 - “is the user visiting this place more or less periodically?” (without knowing the actual period)

Outline

1 Pattern matching

2 Methodology

3 Experiments

4 Perspectives

Untimed pattern matching: example

- Naive algorithm for pattern matching

c r e p e s $\in ?L(\{c|i|d\}^?r^*e)$

Untimed pattern matching: example

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c

Untimed pattern matching: example

- Naive algorithm for pattern matching

c	r	e	p	e	s	$\in ?L(\{c i d\}^?r^*e)$
c	r					

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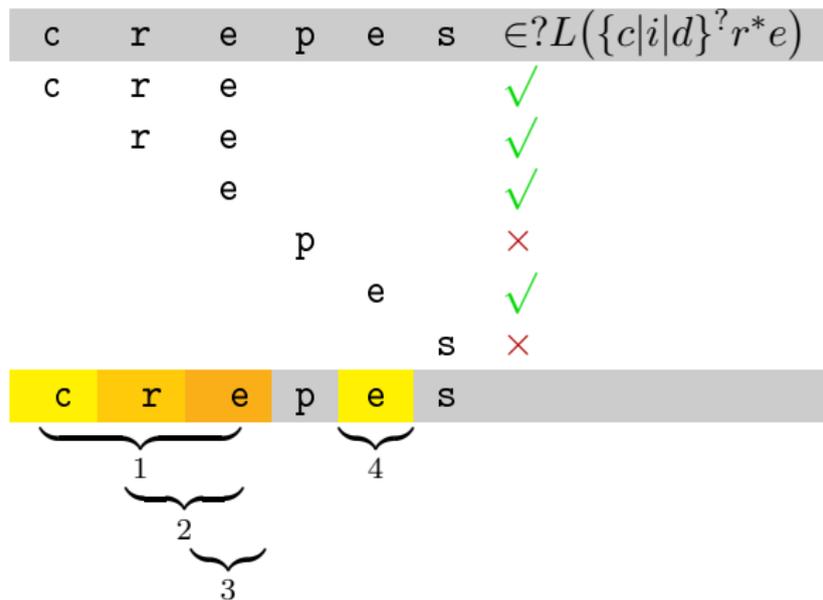
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				e		✓
					s	✗

Untimed pattern matching: example

Naive algorithm for pattern matching



Timed pattern matching: timed word

Timed word

[Alur and Dill, 1994]

=

sequence of **actions** and **timestamps**



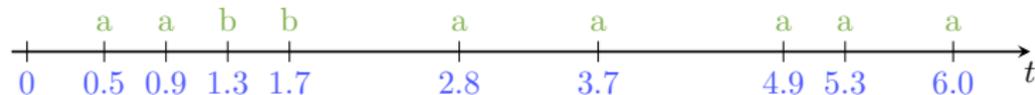
Timed pattern matching: timed word

Timed word

[Alur and Dill, 1994]

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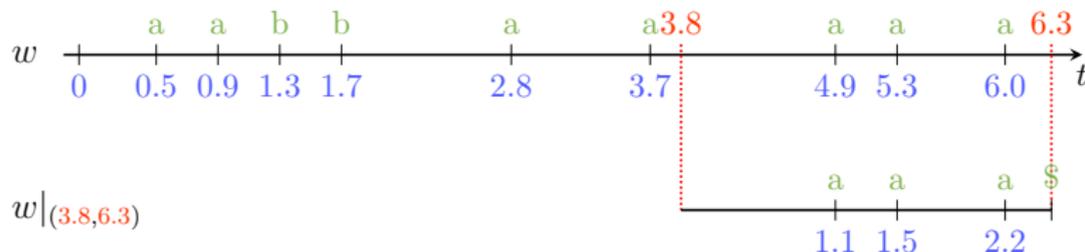


Timed word segment

[Waga et al., 2016]

=

projection of a segment of the timed word onto a given interval



Timed pattern matching: timed automaton

How to express a (timed) property on a log?

Example

“At least 1 time unit after the start of the segment, **a** is observed.
Then, within strictly less than 1 time unit, another **a** is observed.
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Timed pattern matching: timed automaton

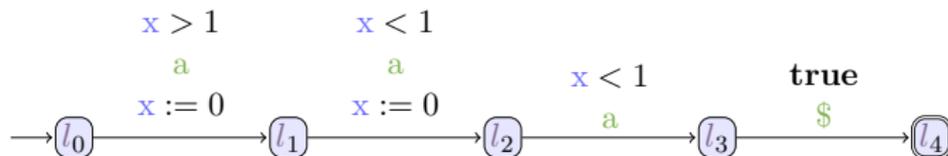
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Then, within strictly less than 1 time unit, another **a** is observed.”

A solution: **timed automata**

[Alur and Dill, 1994]



- expressive
- well-studied
- supported by well-established model-checkers

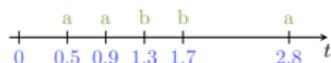
Timed pattern matching: principle

Timed pattern matching

Inputs

A log

(timed word)



Output

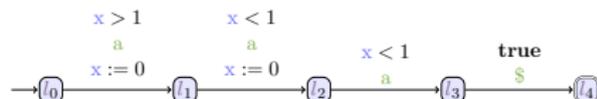
- The set of time intervals where faults are detected
 \Rightarrow Set of **matching intervals** $\{(t, t') \mid w|_{(t,t')} \in \mathcal{L}(\mathcal{A})\}$

A property

usually a specification of **faults**

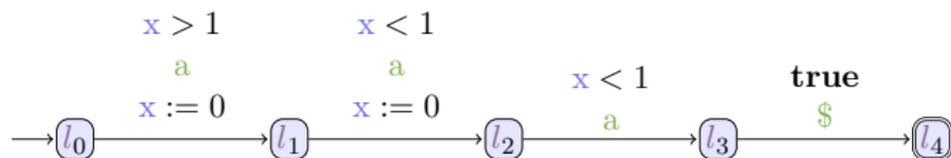
(timed automaton)

[Alur and Dill, 1994]



Timed pattern matching: example

Our property:

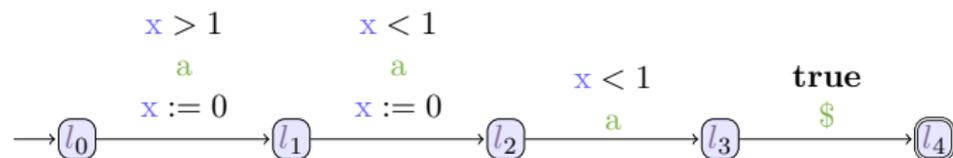


Our log:

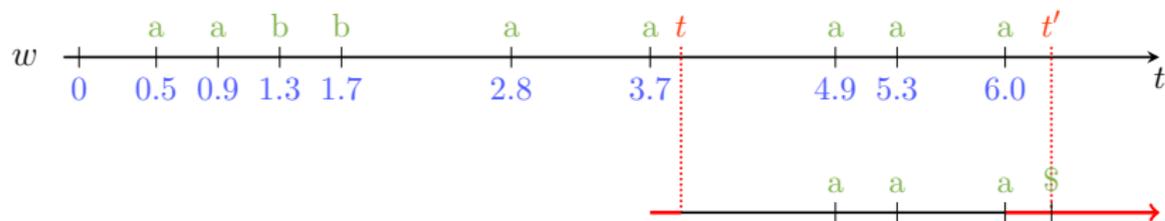


Timed pattern matching: example

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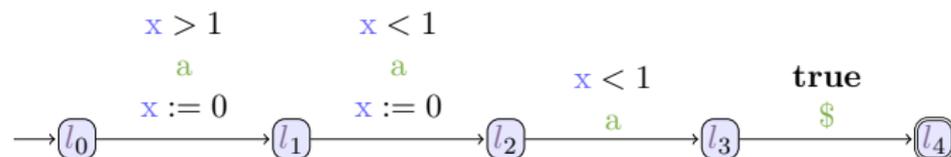


Our log:

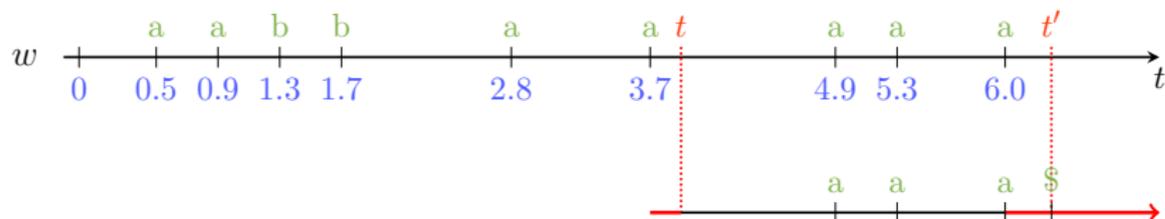


Timed pattern matching: example

Our property:



Our log:



Set of matching intervals:

$$\{(t, t') \mid w|_{(t, t')} \in \mathcal{L}(\mathcal{A})\} = \{(t, t') \mid t \in (3.7, 3.9), t' \in [6.0, \infty)\}$$

Previous works

■ Timed pattern matching with **signals**

[Ulus et al., 2014, Ulus et al., 2016, Ulus, 2017]

- logs are encoded by **signals** (i. e., values that vary over time)
 - *state-based* view, while our timed words are *event-based*
- specification is encoded by timed regular expressions (TREs)

■ Timed pattern matching with timed words and **timed automata**

[Waga et al., 2016, Waga et al., 2017]

- [Waga et al., 2016]: brute-force and Boyer-Moore algorithm
- [Waga et al., 2017]: online algorithm that employs skip values from the Franek–Jennings–Smyth string matching algorithm [Franek et al., 2007]

Goal: Extend timed pattern matching for uncertainty

Challenges

- The property may not be known with full certainty:
 - Detect a periodic event but **without knowing the period**
 - “is the user visiting this place more or less periodically?” (without knowing the actual period)
- Optimization problems
 - Find minimal/maximal timings for which some property holds
 - “what are the minimum/maximum intervals without visiting this shop”?

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Objective

Find intervals of time **and values of parameters** for which a property holds

Outline

1 Pattern matching

2 Methodology

3 Experiments

4 Perspectives

Methodology

Main idea

Use **parametric timed model checking**

- parametric timed automata
- parameter synthesis
- IMITATOR

[Alur et al., 1993]

[André et al., 2012]

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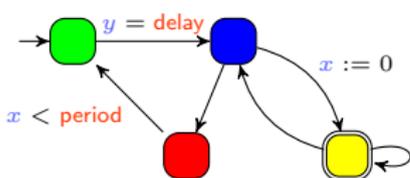
Methodology step by step

- 1 Encode the property using a PTA
- 2 Add two parameters t and t'
- 3 Apply a (mild) transformation to the property a PTA
- 4 Transform the timed word into a PTA
- 5 Perform the composition of both PTA
- 6 Apply reachability synthesis to the product

Outline

- 1 Pattern matching
- 2 Methodology
 - Parametric timed automata
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timed model checking



?

\equiv

 is unreachable

A **property** to be satisfied

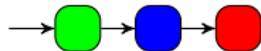
A **model** of the system

- Question: does the model of the system satisfy the property?

Yes

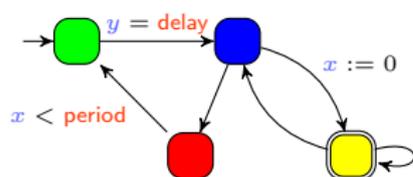


No



Counterexample

Parametric timed model checking



A **model** of the system

?



 is unreachable

A **property** to be satisfied

- Question: for what values of the parameters does the model of the system satisfy the property?

Yes if...



$$2\text{delay} > \text{period} \\ \wedge \text{period} < 20.46$$

Property: parametric timed automaton

Expressing a **parametric timed** property on a log

Example

“At least p_1 time units after the start of the segment, **a** is observed.
Then, within strictly less than p_2 time units, another **a** is observed.
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Property: parametric timed automaton

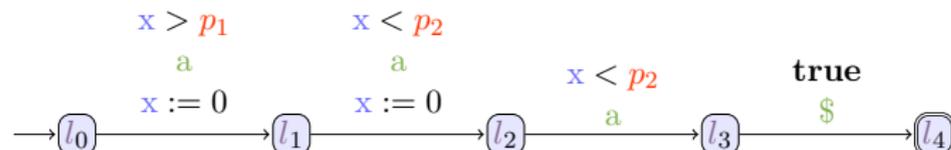
Expressing a **parametric timed** property on a log

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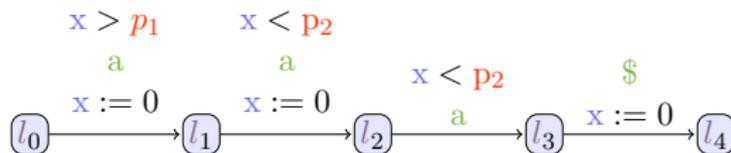
Our solution: **parametric timed automata**

[Alur et al., 1993]



Modifying the property pattern

Add some start and end gadgets for completeness of the method

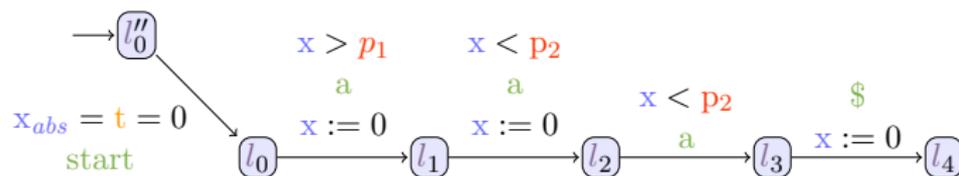


See manuscript for formal transformation and proofs

Modifying the property pattern

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- 1 Add an initial transition in o-time
 - Captures segments starting from o

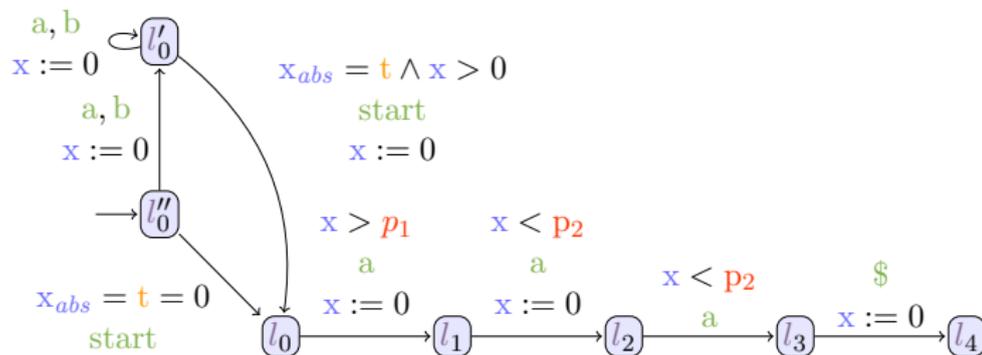


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- 1 Add an initial transition in o-time
 - Captures segments starting from o
- 2 Add a new location with a self-loop
 - Captures segments not starting from the beginning of the word

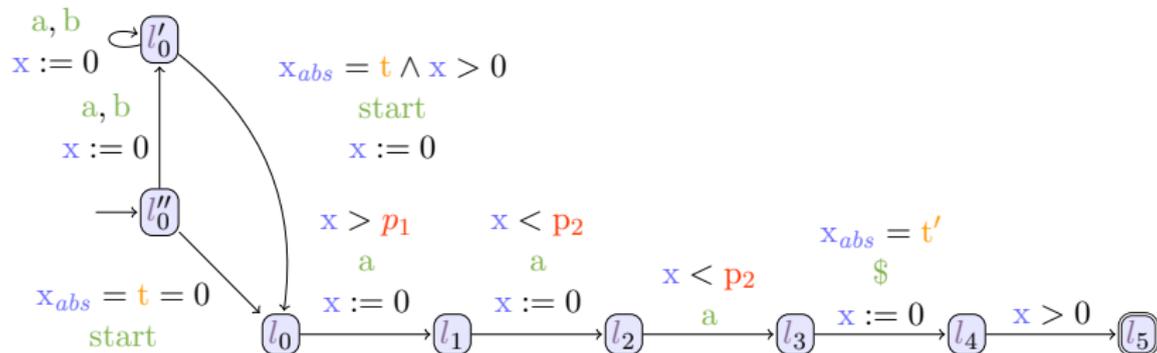


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Modifying the property pattern

Add some start and end gadgets for completeness of the method

- 1 Add an initial transition in 0-time
 - Captures segments starting from 0
- 2 Add a new location with a self-loop
 - Captures segments not starting from the beginning of the word
- 3 Add a new final transition in > 0 time
 - To match the usual definition that the segment must end in > 0 time after the last action



See manuscript for formal transformation and proofs

Transforming a log into a (parametric) timed automaton

Essentially easy:

- 1 Add one clock never reset (**absolute time**)
- 2 Convert pairs (**action**, **time**) into transitions

Transforming a log into a (parametric) timed automaton

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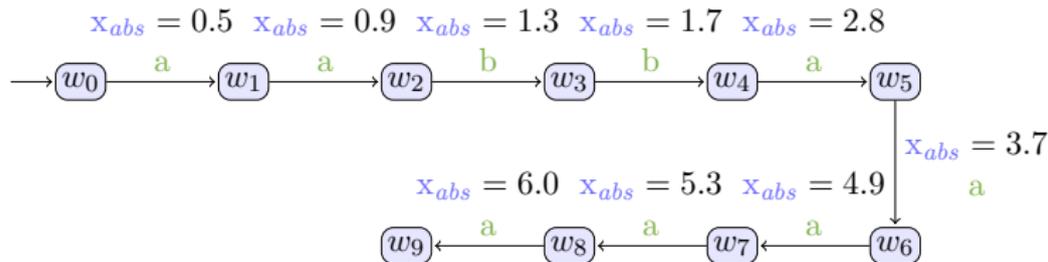
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Product and reachability synthesis

Result

The set of parameter valuations $t, t', p_1, p_2 \dots$ reaching the final location of the property is **exactly the answer** to the parametric pattern matching problem

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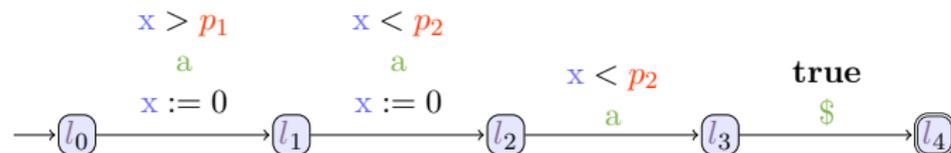
Remark

This problem is **decidable**... in contrast to most problems using PTAs!

[André, 2018]

Product and reachability synthesis: example

Our property:

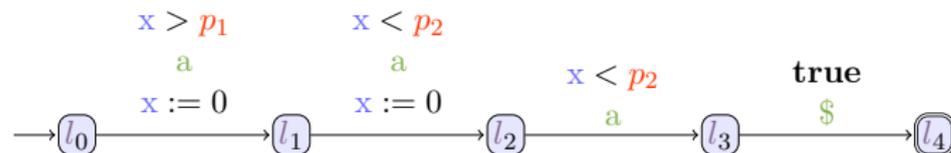


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Product and reachability synthesis: example

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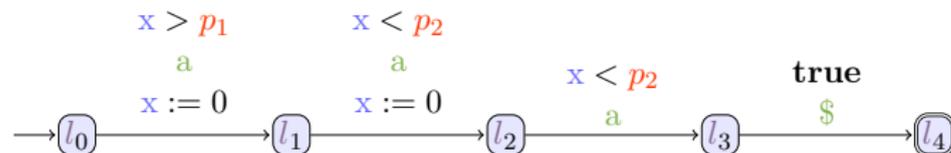


Set of matching intervals:

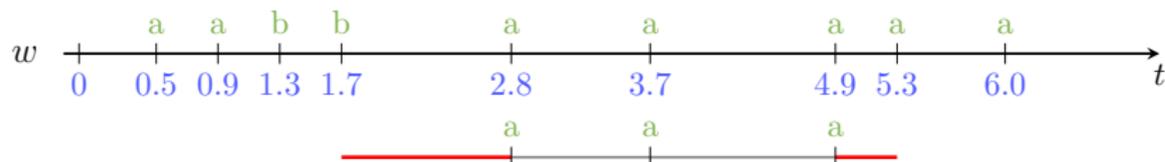
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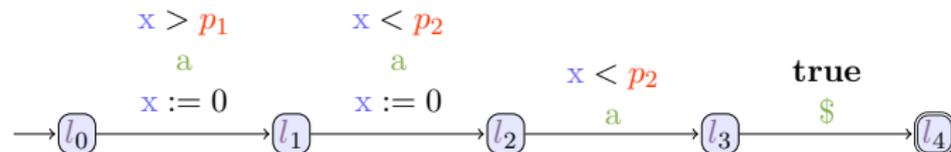


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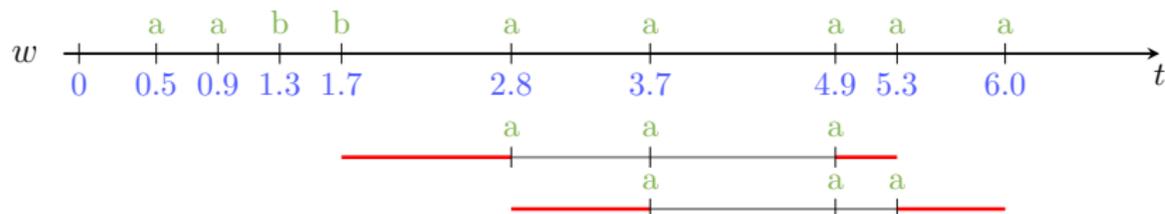
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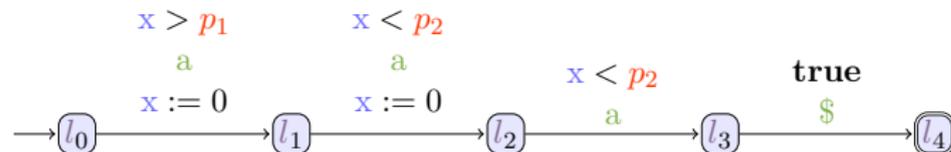


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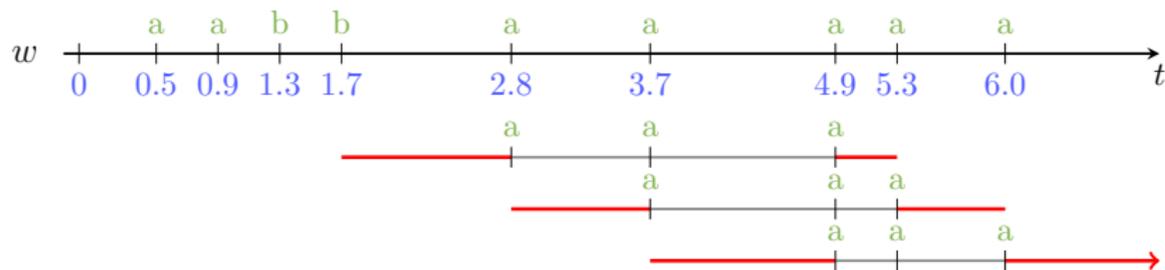
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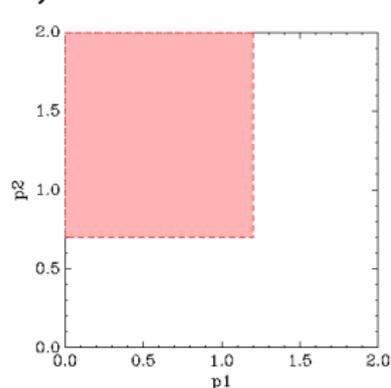
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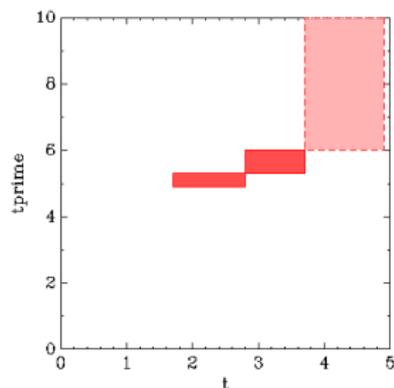
Example: graphical representation

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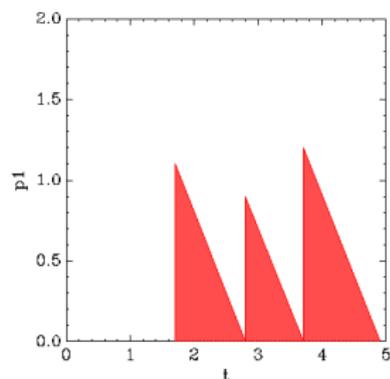
Projections in 2 dimensions:



On p_1 and p_2



On t and t'



On t and p_1

Outline

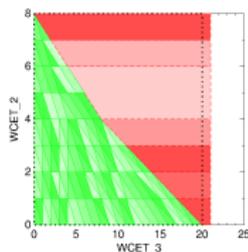
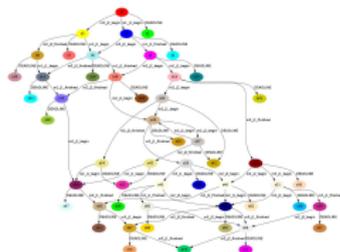
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Outline

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 - IMITATOR in a nutshell
 - Benchmarks
- 4 Perspectives

IMITATOR

- A tool for modeling and verifying **timed concurrent systems** with unknown constants modeled with **parametric timed automata**
 - Communication through (strong) broadcast synchronization
 - Rational-valued shared discrete variables
 - **Stopwatches**, to model schedulability problems with preemption
- Synthesis algorithms
 - (non-Zeno) parametric model checking (using a subset of **TCTL**)
 - Language and trace preservation, and robustness analysis
 - Parametric deadlock-freeness checking



IMITATOR

Under continuous development since 2008

[André et al., FM'12]

A library of benchmarks

- Communication protocols
- Schedulability problems
- Asynchronous circuits
- ...and more

Free and open source software: Available under the GNU-GPL license



IMITATOR

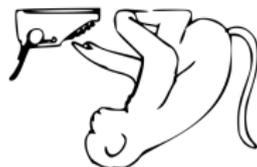
Under continuous development since 2008

[André et al., FM'12]

A library of benchmarks

- Communication protocols
- Schedulability problems
- Asynchronous circuits
- ...and more

Free and open source software: Available under the GNU-GPL license



Try it!

www.imitator.fr

Some success stories

- Modeled and verified an **asynchronous memory circuit** by ST-Microelectronics
- Parametric schedulability analysis of a prospective architecture for the flight control system of the **next generation of spacecrafts** designed at ASTRIUM Space Transportation [Fribourg et al., 2012]
- Verification of software product lines [Luthmann et al., 2017]
- Formal timing analysis of **music scores** [Fanchon and Jacquemard, 2013]
- Solution to a challenge related to a **distributed video processing system** by Thales
- **Offline monitoring**

Outline

- 1 Pattern matching
- 2 Methodology
- 3 Experiments**
 - IMITATOR in a nutshell
 - Benchmarks**
- 4 Perspectives

Experimental environment

Toolkit

- Simple Python script to transform timed words into IMITATOR PTAs
- Slightly modified version of IMITATOR
 - To handle PTAs with dozens of thousands of locations
 - To manage n -parameter constraints with dozens of thousands of disjuncts

Sources, binaries, models, logs can be found at www.imitator.fr/static/ICECCS18

Case study 1: GEAR (description)

Monitoring the gear change of an automatic transmission system

- Obtained by simulation of the Simulink model of an automatic transmission system [Hoxha et al., 2014]
- S-TaLiRo [Annpureddy et al., 2011] used to generate an input to this model (generates a gear change signal that is fed to the model)
- Gear chosen from $\{g_1, g_2, g_3, g_4\}$
- Generated gear change recorded in a **timed word**

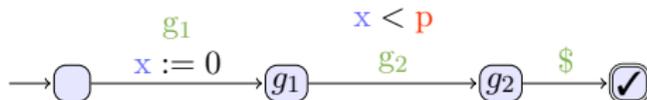
Property

“If the gear is changed to 1, it should not be changed to 2 within p seconds.”

This condition is related to the requirement ϕ_5^{AT} proposed in [Hoxha et al., 2014] (the nominal value for p in [Hoxha et al., 2014] is 2).

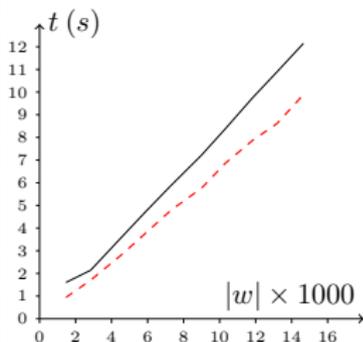
Case study 1: GEAR (experiments)

Property: “If the gear is changed to 1, it should not be changed to 2 within p seconds.”



Experiments data:

Model		PTPM				PTPM _{opt}	
Length	Time frame	States	Matches	Parsing (s)	Comp. (s)	States	Comp. (s)
1,467	1,000	4,453	379	0.02	1.60	3,322	0.94
2,837	2,000	8,633	739	0.33	2.14	6,422	1.70
4,595	3,000	14,181	1,247	0.77	3.63	10,448	2.85
5,839	4,000	17,865	1,546	1.23	4.68	13,233	3.74
7,301	5,000	22,501	1,974	1.94	5.88	16,585	4.79
8,995	6,000	27,609	2,404	2.96	7.28	20,413	5.76
10,316	7,000	31,753	2,780	4.00	8.38	23,419	6.86
11,831	8,000	36,301	3,159	5.39	9.75	26,832	7.87
13,183	9,000	40,025	3,414	6.86	10.89	29,791	8.61
14,657	10,000	44,581	3,816	8.70	12.15	33,141	9.89



PTPM_{opt}: alternative procedure to find the minimum/maximum value of a parameter along the log

Case study 2: ACCEL (description)

Monitoring the acceleration of an automated transmission system

- Also obtained by simulation from the Simulink model of [Hoxha et al., 2014]
- (discretized) value of three state variables recorded in the log:
 - engine RPM (discretized to “high” and “low” with a certain threshold)
 - velocity (discretized to “high” and “low” with a certain threshold)
 - 4 gear positions

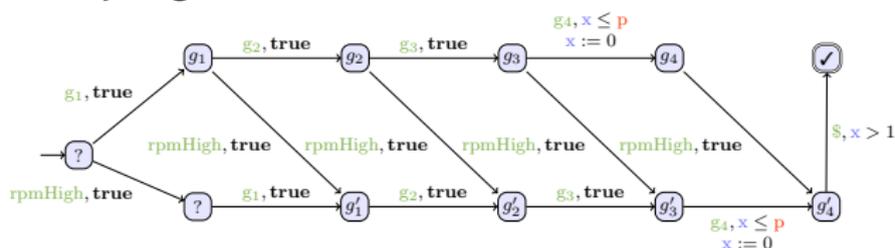
Property

“If a gear changes from 1 to 2, 3, and 4 in this order in p seconds and engine RPM becomes large during this gear change, then the velocity of the car must be sufficiently large in one second.”

This condition models the requirement ϕ_8^{AT} proposed in [Hoxha et al., 2014] (the nominal value for p in [Hoxha et al., 2014] is 10).

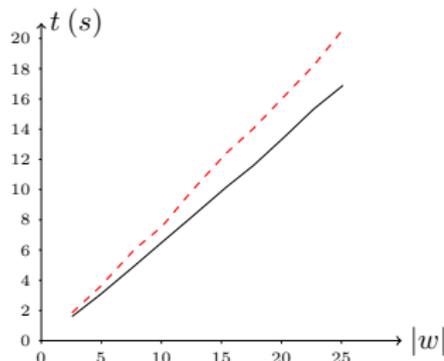
Case study 2: ACCEL (experiments)

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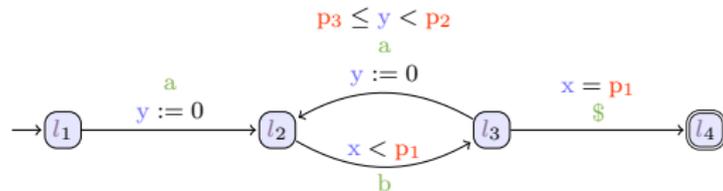
Experiments data:

Model		PTPM			PTPM _{opt}		
Length	Time frame	States	Matches	Parsing (s)	Comp. (s)	States	Comp. (s)
2,559	1,000	6,504	2	0.27	1.60	6,502	1.85
4,894	2,000	12,429	2	0.86	3.04	12,426	3.57
7,799	3,000	19,922	7	2.21	4.98	19,908	6.06
10,045	4,000	25,520	3	3.74	6.51	25,514	7.55
12,531	5,000	31,951	9	6.01	8.19	31,926	9.91
15,375	6,000	39,152	7	9.68	10.14	39,129	12.39
17,688	7,000	45,065	9	13.40	11.61	45,039	14.06
20,299	8,000	51,660	10	18.45	13.52	51,629	16.23
22,691	9,000	57,534	11	24.33	15.33	57,506	18.21
25,137	10,000	63,773	13	31.35	16.90	63,739	20.61



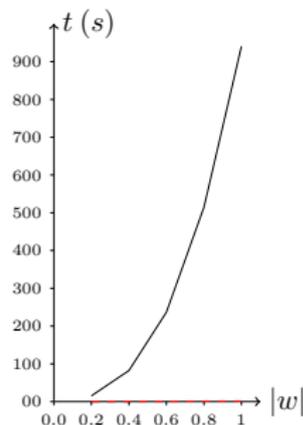
Case study 3: BLOWUP

Property made on purpose to test our scalability



Experiments data:

Model		PTPM				PTPM _{opt}	
Length	Time frame	States	Matches	Parsing (s)	Comp. (s)	States	Comp. (s)
200	101	20,602	5,050	0.01	15.31	515	0.24
400	202	81,202	20,100	0.02	82.19	1,015	0.49
600	301	181,802	45,150	0.03	236.80	1,515	0.71
800	405	322,402	80,200	0.05	514.57	2,015	1.05
1,000	503	503,002	125,250	0.06	940.74	2,515	1.24



Outline

- 1 Pattern matching
- 2 Methodology
- 3 Experiments
- 4 Perspectives**

Summary

- New method to monitor logs of real-time systems
- Methodology: parametric timed model checking
- Applications: automotive industry
 - **Linear** in the size of the log
 - Able to handle logs of dozens of thousands of events

Summary

- New method to monitor logs of real-time systems
- Methodology: parametric timed model checking
- Applications: automotive industry
 - **Linear** in the size of the log
 - Able to handle logs of dozens of thousands of events
- Article **Offline timed pattern matching under uncertainty** by André, Hasuo and Waga to be presented at ICECCS 2018 (December)
- An **offline** online algorithm
 - We believe our algorithm is in fact essentially **online**
 - No need for the whole log to start the analysis
 - The word could be fed to IMITATOR in an incremental manner
 - But the speed may need to be improved further

Perspectives

■ Extensions

- Improve the efficiency with **skipping**
- Exploit the **polarity of parameters**
- Use and extend the MONAA library

[Waga et al., 2017]

[Asarin et al., 2011]

[Waga et al., 2018]

■ Graphical representation and interpretation

- How to interpret dozens of thousands of matches?

Perspectives

■ Extensions

- Improve the efficiency with **skipping**
- Exploit the **polarity of parameters**
- Use and extend the MONAA library

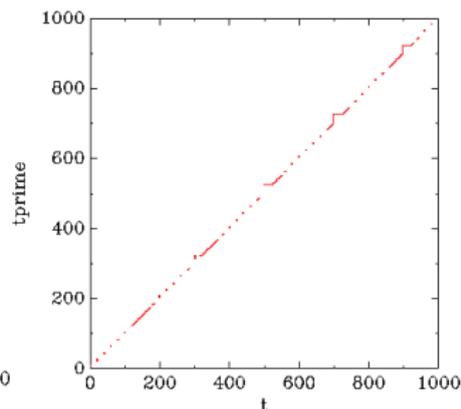
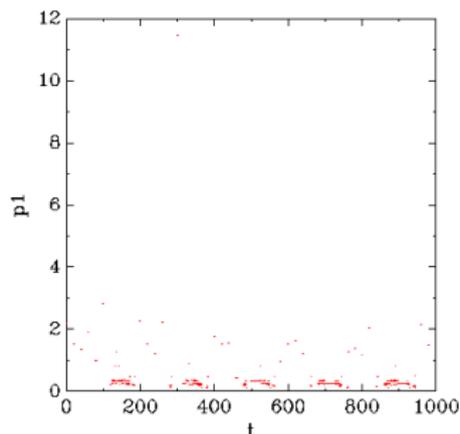
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■ Graphical representation and interpretation

- How to interpret dozens of thousands of matches?



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MONAA: A tool for timed pattern matching with automata-based acceleration.

In *MT@CPSWeek*, pages 14–15. IEEE.

Additional explanation

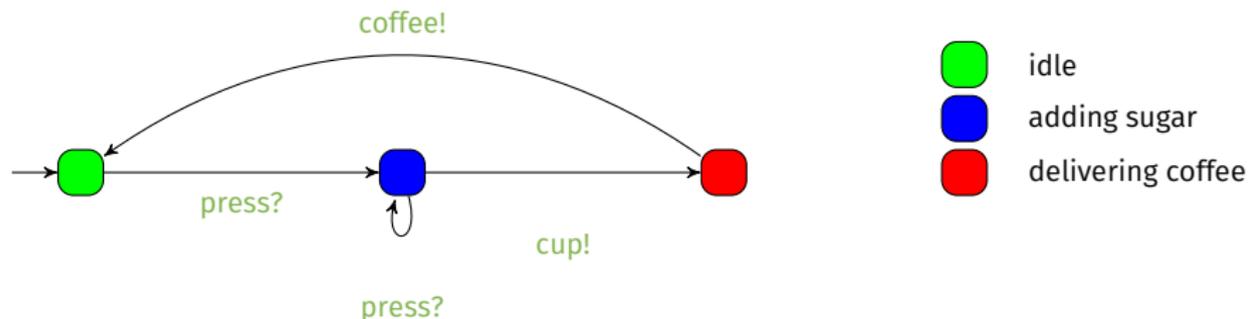
Timed automaton (TA)

- Finite state automaton (sets of locations)



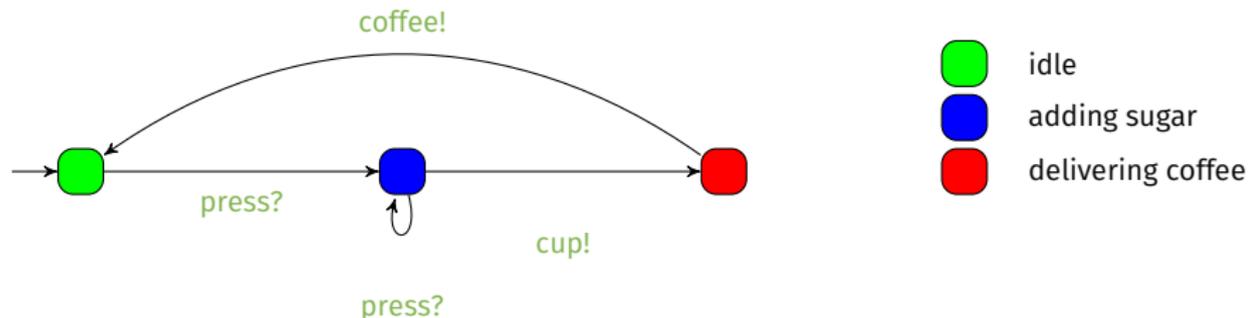
Timed automaton (TA)

- Finite state automaton (sets of locations and actions)



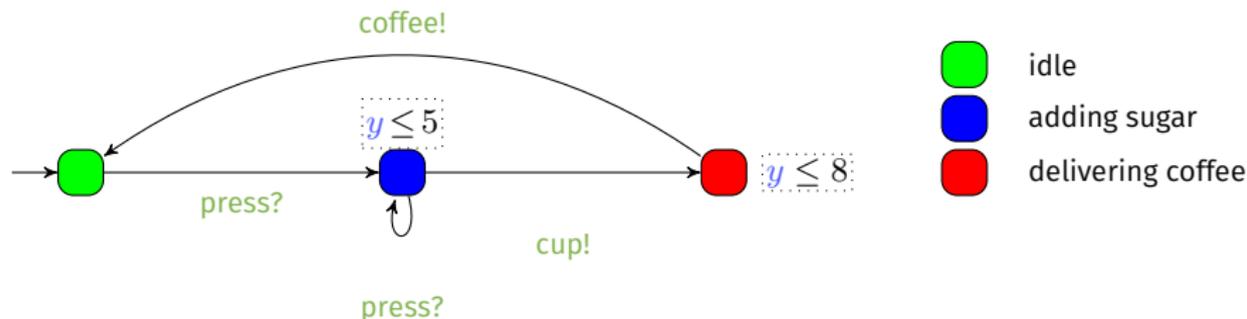
Timed automaton (TA)

- Finite state automaton (sets of **locations** and **actions**) augmented with a set X of **clocks** [Alur and Dill, 1994]
 - Real-valued variables evolving linearly **at the same rate**



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- Finite state automaton (sets of **locations** and **actions**) augmented with a set X of **clocks** [Alur and Dill, 1994]
 - Real-valued variables evolving linearly **at the same rate**
 - Can be compared to integer constants in invariants
- Features
 - Location **invariant**: property to be verified to stay at a location



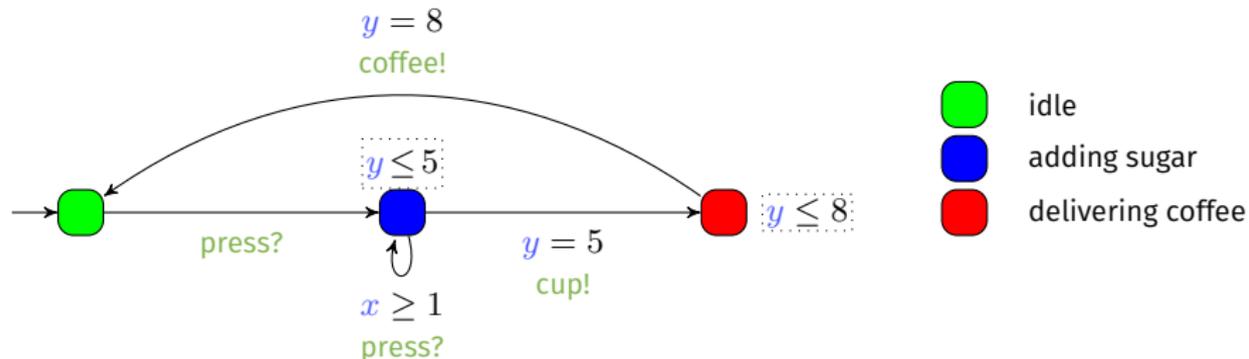
Timed automaton (TA)

- Finite state automaton (sets of **locations** and **actions**) augmented with a set X of **clocks** [Alur and Dill, 1994]

- Real-valued variables evolving linearly **at the same rate**
- Can be compared to integer constants in invariants and guards

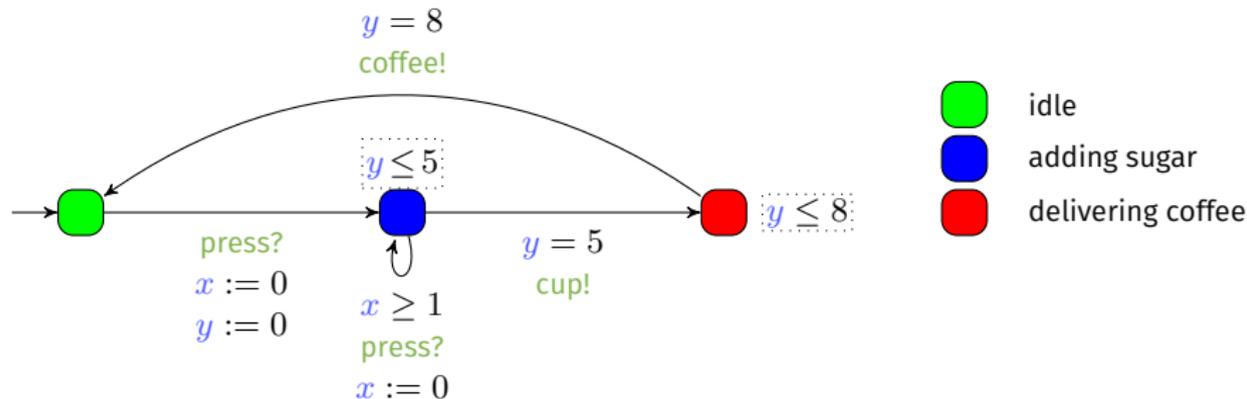
■ Features

- Location **invariant**: property to be verified to stay at a location
- Transition **guard**: property to be verified to enable a transition

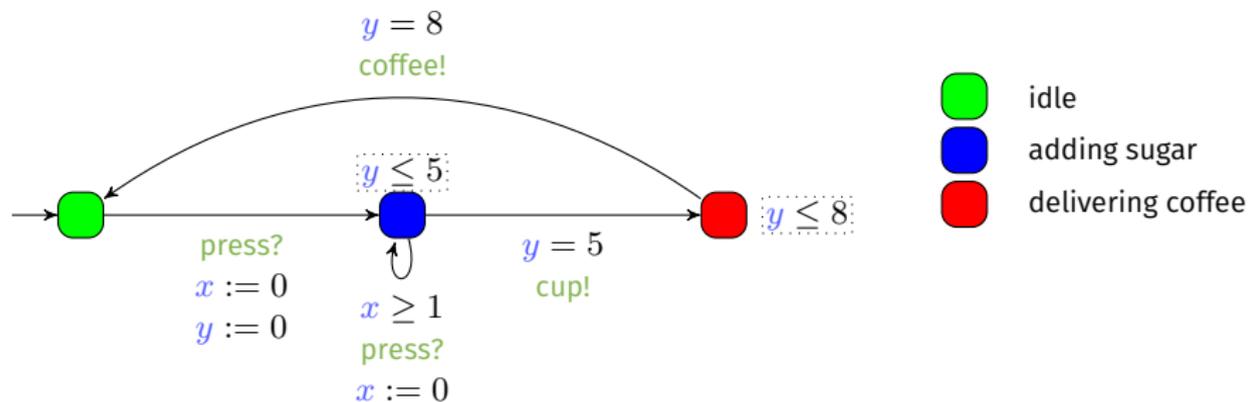


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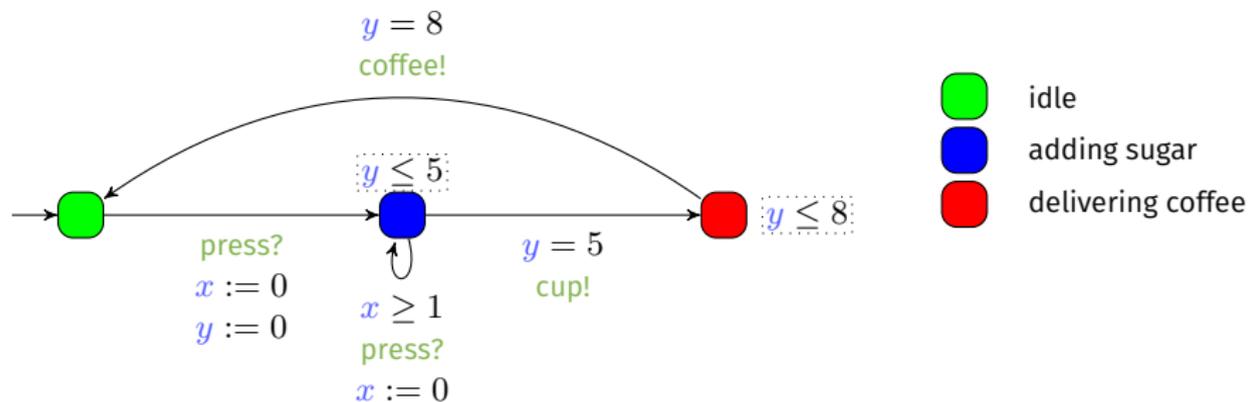
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 - Can be compared to integer constants in invariants and guards
- Features
 - Location **invariant**: property to be verified to stay at a location
 - Transition **guard**: property to be verified to enable a transition
 - Clock **reset**: some of the clocks can be **set to 0** along transitions



The most critical system: The coffee machine



The most critical system: The coffee machine

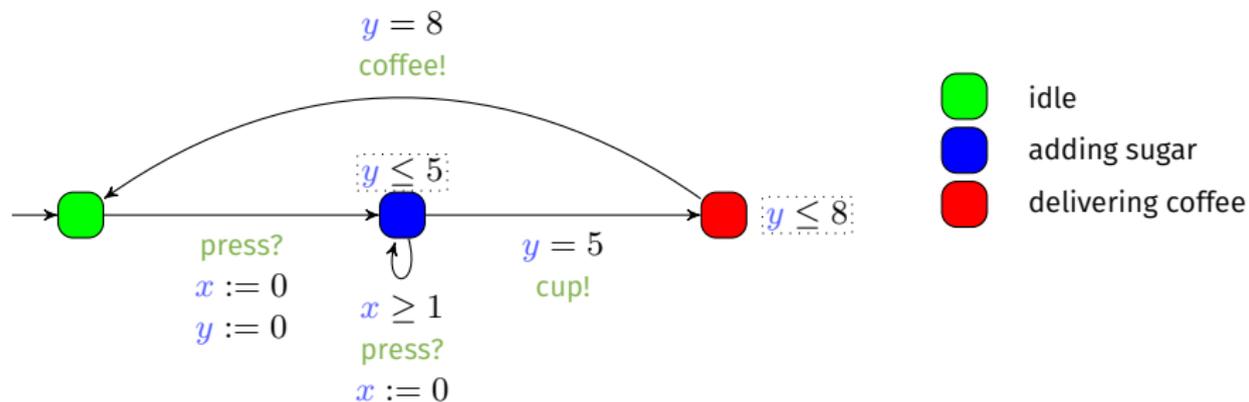


Example of concrete run for the coffee machine

Coffee with 2 doses of sugar

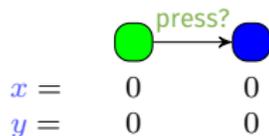

 $x = 0$
 $y = 0$

The most critical system: The coffee machine

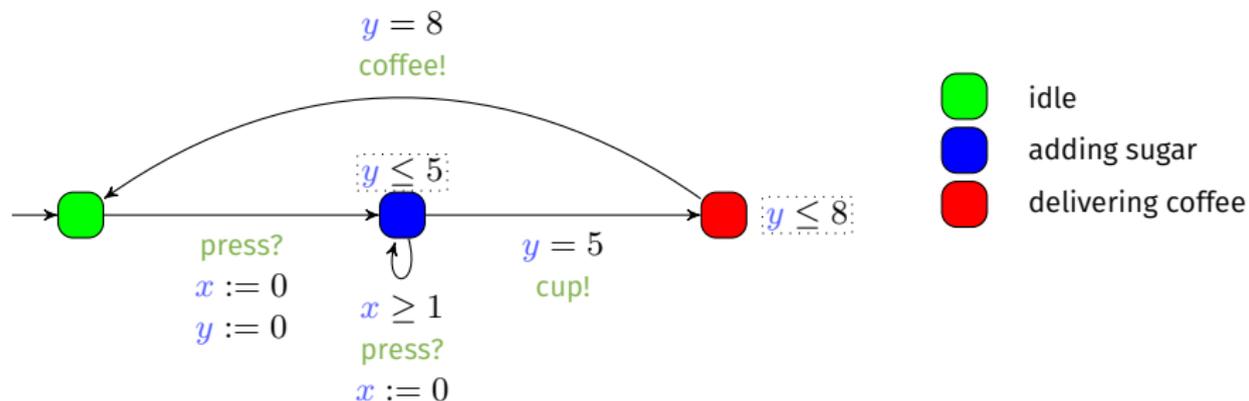


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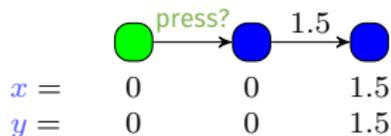


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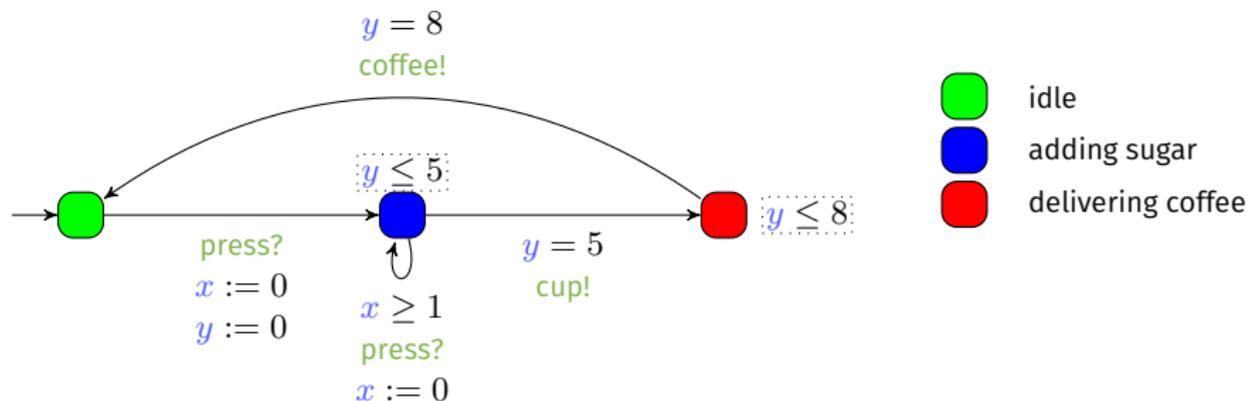


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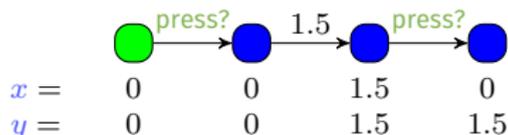


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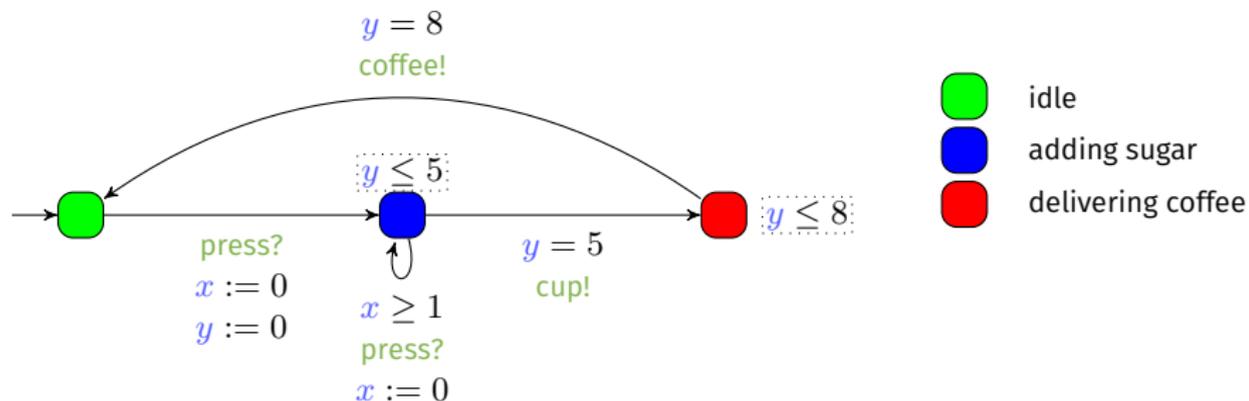


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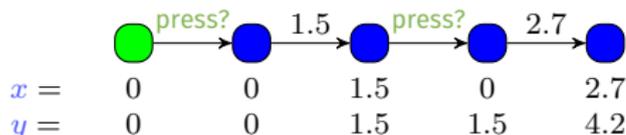


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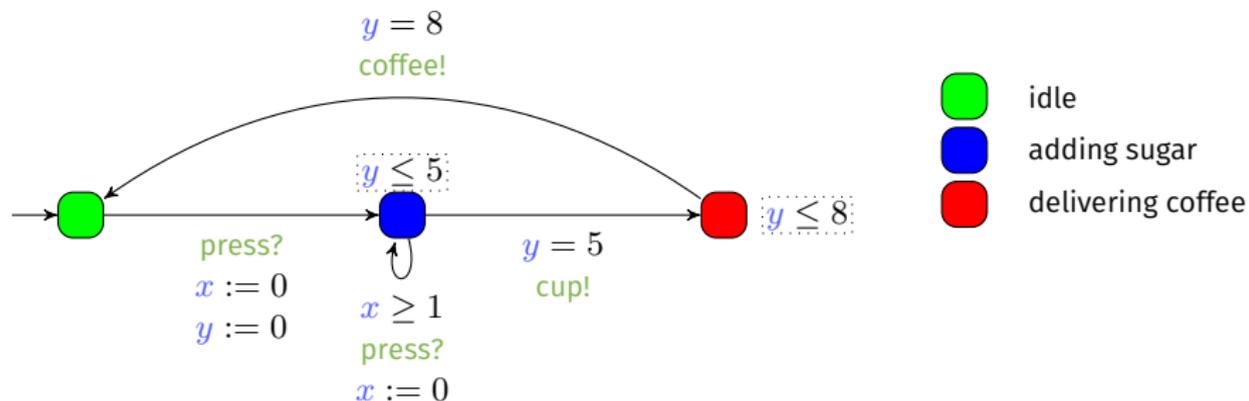


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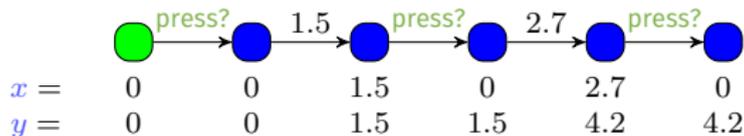


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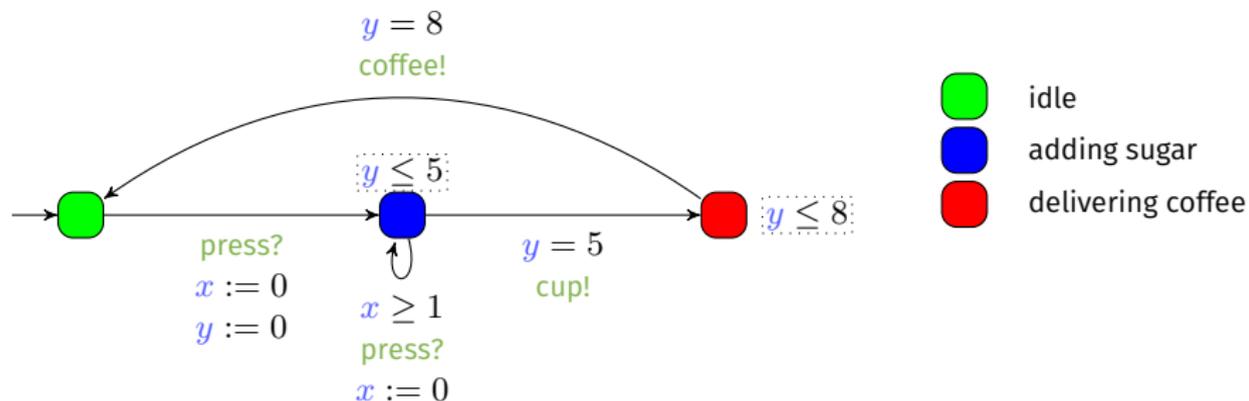


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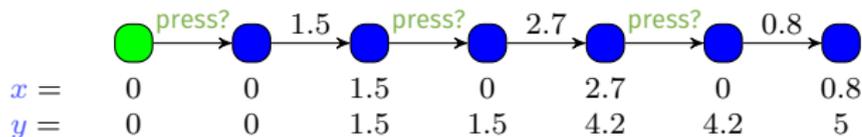


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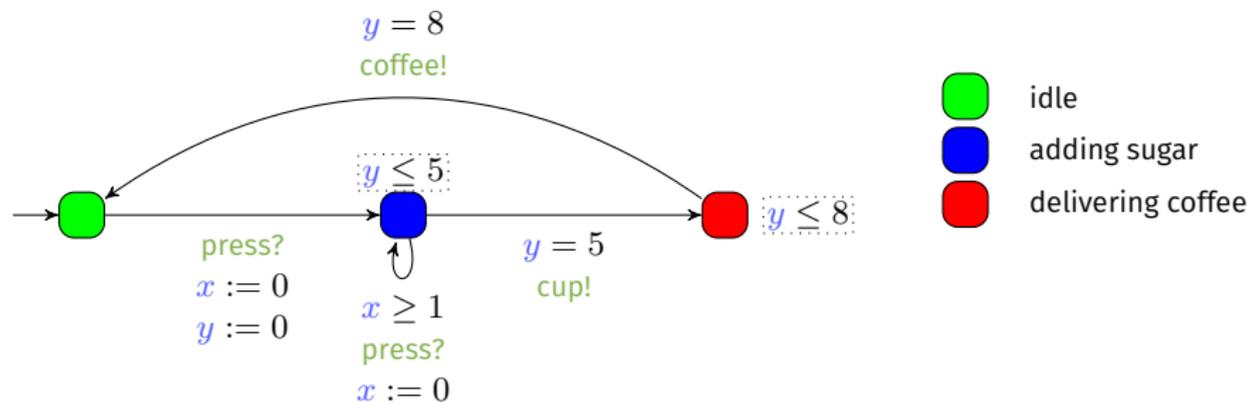


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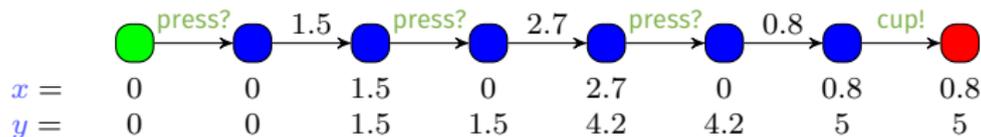


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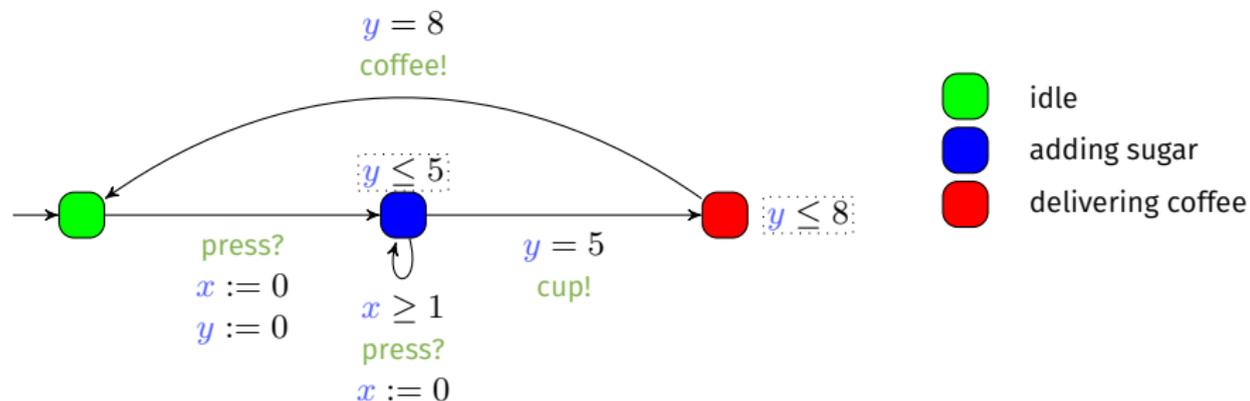


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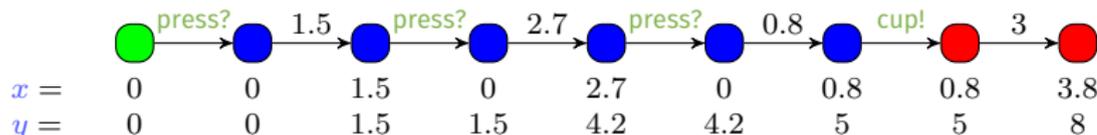


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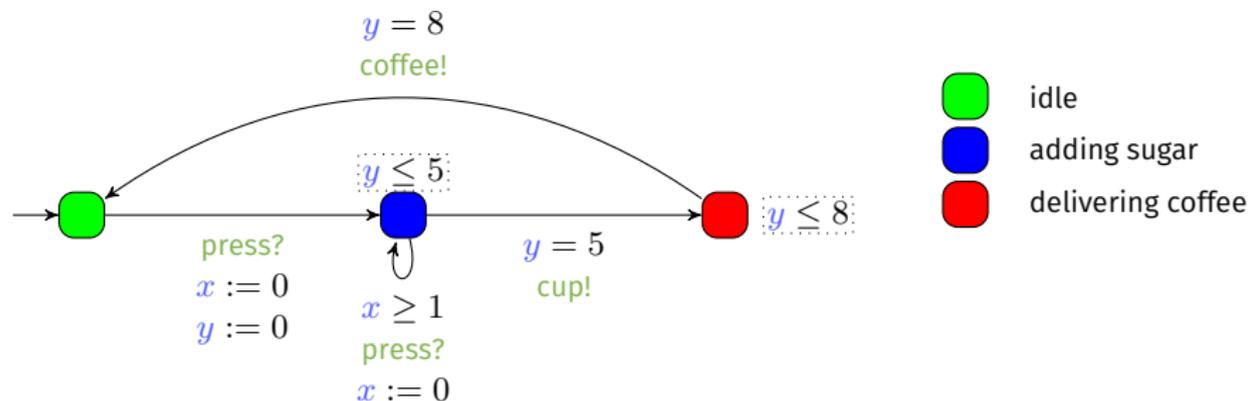


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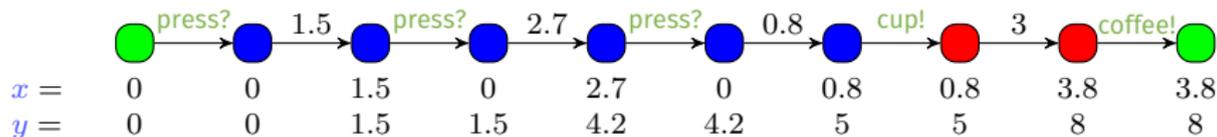


The most critical system: The coffee machine



Example of concrete run for the coffee machine

Coffee with 2 doses of sugar



Concrete semantics of timed automata

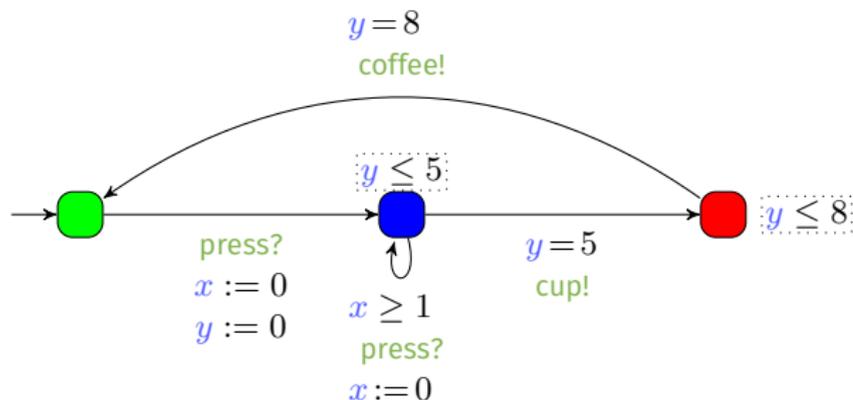
- **Concrete state** of a TA: pair (l, w) , where
 - l is a location,
 - w is a **valuation** of each clock

Example: $(\bullet, (x=1.2, y=3.7))$

- **Concrete run**: alternating sequence of **concrete states** and **actions** or **time elapse**

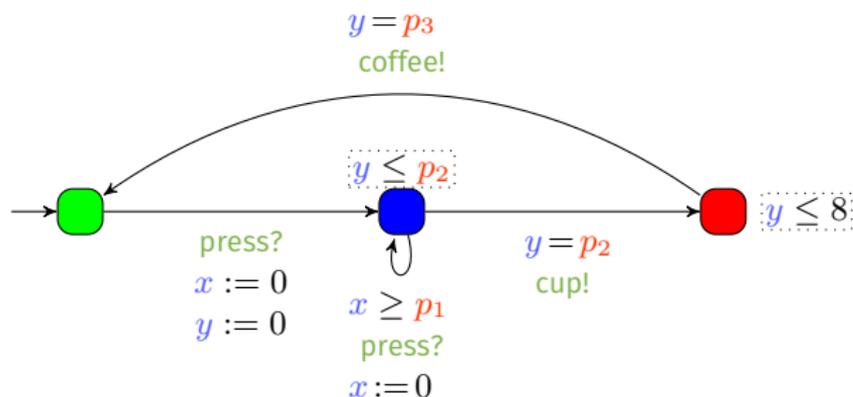
Parametric Timed Automaton (PTA)

- Timed automaton (sets of locations, actions and clocks)



Parametric Timed Automaton (PTA)

- Timed automaton (sets of locations, actions and clocks) augmented with a set P of parameters [Alur et al., 1993]
 - Unknown constants compared to a clock in guards and invariants



Symbolic semantics of parametric timed automata

- **Symbolic state** of a PTA: pair (l, C) , where
 - l is a location,
 - C is a convex polyhedron over X and P with a special form, called **parametric zone** [Hune et al., 2002]

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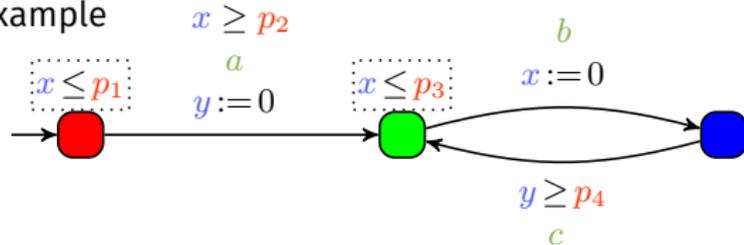
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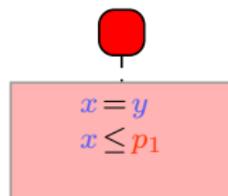
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- [Hune et al., 2002]

- **Symbolic run**: alternating sequence of **symbolic states** and **actions**

- **Example**



- Possible symbolic run for this PTA



Symbolic semantics of parametric timed automata

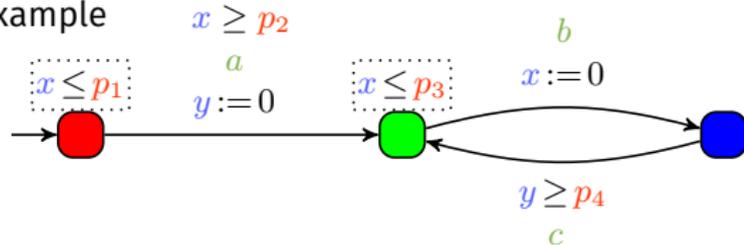
- **Symbolic state** of a PTA: pair (l, C) , where

- l is a location,
- C is a convex polyhedron over X and P with a special form, called **parametric zone**

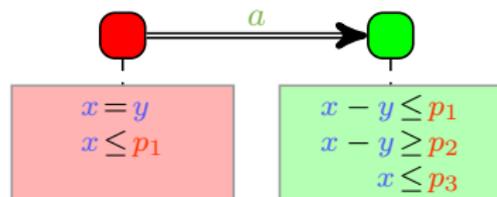
[Hune et al., 2002]

- **Symbolic run**: alternating sequence of **symbolic states** and **actions**

- **Example**



- Possible symbolic run for this PTA



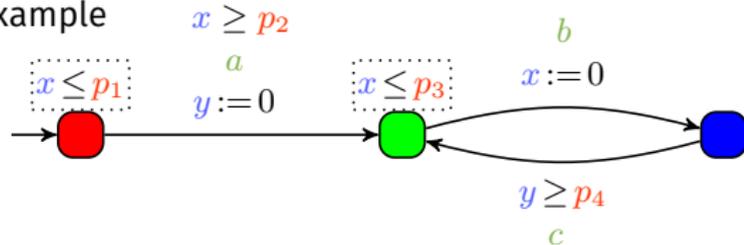
Symbolic semantics of parametric timed automata

- **Symbolic state** of a PTA: pair (l, C) , where

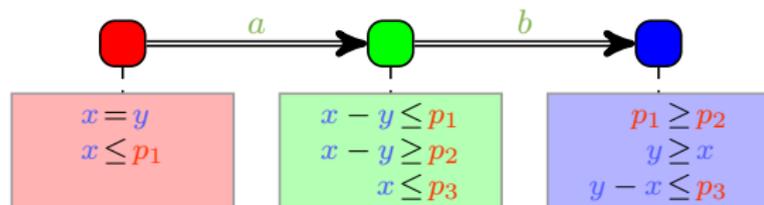
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- **Example**



- Possible symbolic run for this PTA



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