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Parametric Timed Model Checking for Guaranteeing Timed Opacity

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PTA for Guaranteeing Timed Opacity



Context: side-channel attacks

Threats to a system using non-algorithmic weaknesses

- Cache attack
- Electromagnetic attacks
- Power attacks



- Acoustic attacks
- Timing attacks
- etc.
- Example
 - Number of pizzas (and order time) ordered by the white house prior to major war announcements¹

¹http://home.xnet.com/~warinner/pizzacites.html

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Context: timing attacks

Principle: deduce private information from timing data (execution time)

Issues:

May depend on the implementation (or, even worse, be introduced by the compiler)

 A relatively trivial solution: make the program last always its maximum execution time
 Drawback: loss of efficiency

 \rightsquigarrow Non-trivial problem

```
1 # input pwd : Real password
2 # input attempt: Tentative password
3 for i = 0 to min(len(pwd, len(attempt)) - 1 do
4 if pwd[i] =/= attempt[i] then
5 return false
6 done
7 return true
```



pwd	с	h	0	u	d	0	u	f	u
attempt	с	h	е	е	S	е			

Execution time:





Execution time: ϵ





Execution time: $\epsilon + \epsilon$





Execution time: $\epsilon + \epsilon + \epsilon$





Execution time: $\epsilon + \epsilon + \epsilon$

Problem: The execution time is proportional to the number of consecutive correct characters from the beginning of attempt

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Outline

1 Problems

2 Timed automata

- 3 Timed-opacity computation
- 4 Timed-opacity synthesis

5 Experiments

6 Conclusion and perspectives

Informal problems

Question: can we exhibit secure execution times?

Time-opacity computation

Exhibit execution times for which it is not only possible to infer information on the internal behavior

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Time-opacity computation

Exhibit execution times for which it is not only possible to infer information on the internal behavior

Further question: can we also tune internal timing constants to make the system resisting to timing attacks?

Time-opacity synthesis

Exhibit execution times and internal timing constants for which it is not only possible to infer information on the internal behavior

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Finite state automaton (sets of locations)



Finite state automaton (sets of locations and actions)



- Finite state automaton (sets of locations and actions) augmented with a set X of clocks
 [Alur and Dill, 1994]
 - Real-valued variables evolving linearly at the same rate



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- Features
 - Location invariant: property to be verified to stay at a location



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- Features
 - Location invariant: property to be verified to stay at a location
 - Transition guard: property to be verified to enable a transition
 - Clock reset: some of the clocks can be set to 0 along transitions



Concrete semantics of timed automata

Concrete state of a TA: pair (ℓ, w) , where



Concrete run: alternating sequence of concrete states and actions or time elapse





Example of concrete run for the coffee machine



 $\begin{array}{c} x = 0 \\ y = 0 \end{array}$



















idle adding sugar delivering coffee





Example of concrete run for the coffee machine



idle adding sugar delivering coffee



Example of concrete run for the coffee machine



idle

adding sugar

delivering coffee



Example of concrete run for the coffee machine





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Formalization

Hypotheses:

- A start location ℓ_0 and an end location ℓ_f
- A special private location ℓ_{priv}



Definition (timed opacity)

The system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f if

- for any run to ℓ_f of duration d passing by ℓ_{priv} , there exists another run to ℓ_f of duration d not passing by ℓ_{priv} , and
- 2 conversely

Problem 1: timed-opacity computation

Timed-opacity computation problem

Find durations d ("execution times") of runs from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

Problem 1: timed-opacity computation

Timed-opacity computation problem

Find durations d ("execution times") of runs from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

Example:


Problem 1: timed-opacity computation

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Find durations d ("execution times") of runs from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f



Here, only computations with durations $d \in [2,3]$ are opaque

Problem 1b: timed-opacity

Definition (Timed-opacity)

A system is timed-opaque if the answer to the timed-opacity computation problem is the set of all possible execution times for this system.

Intuition: is a system timed-opaque for all its execution times?

Problem 1b: timed-opacity

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Problem 1b: timed-opacity

Definition (Timed-opacity)

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Here, only computations with durations $\textbf{\textit{d}} \in [2,3]$ are opaque All execution times: [1,3]

ightarrow not timed-opaque

Timed-opacity computation can be achieved

Theorem (Computability of timed-opacity)

The answer to the timed-opacity computation problem can be effectively be computed in the form of a finite union of intervals

Proof: based on the region graph (see paper)

Exact complexity: unproved (EXPSACE upper bound proved, but exponential hardness seems likely)

Remark: to be put in perspective with [Cassez, 2009]

undecidability for a less expressive class, for a stronger notion of opacity

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Towards a more abstract framework...

Problems

- Can we tune some timing constants to guarantee opacity?
- Verification for one set of constants does not usually guarantee the correctness for other values
- **Robustness** [Bouyer et al., 2013]: What happens if 50 is implemented with 49.99?

Towards a more abstract framework...

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- Can we tune some timing constants to guarantee opacity?
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- **Robustness** [Bouyer et al., 2013]: What happens if 50 is implemented with 49.99?

A solution:

Parameter synthesis

Consider that timing constants are unknown constants (parameters)

Parametric Timed Automaton (PTA)

Timed automaton (sets of locations, actions and clocks)



Parametric Timed Automaton (PTA)

- Timed automaton (sets of locations, actions and clocks) augmented with a set P of parameters
 [Alur et al., 1993]
 - Unknown constants compared to a clock in guards and invariants



Notation: Valuation of a PTA

Given a PTA A and a parameter valuation v, we denote by v(A) the (non-parametric) timed automaton where each parameter p is valuated by v(p)

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Given a PTA \mathcal{A} and a parameter valuation v, we denote by $v(\mathcal{A})$ the (non-parametric) timed automaton where each parameter p is valuated by v(p)



Problem 2: timed-opacity synthesis

Timed-opacity synthesis problem

Find parameter valuations v and durations d ("execution times") of runs of v(A) from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

Problem 2: timed-opacity synthesis

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Find parameter valuations v and durations d ("execution times") of runs of v(A) from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

Example: $x \leq 3$ $x \geq p_1$ ℓ_{priv} $x \geq p_2$ ℓ_{priv}

Problem 2: timed-opacity synthesis

Timed-opacity synthesis problem

Find parameter valuations v and durations d ("execution times") of runs of v(A) from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

Example: $x \leq 3$ $x \geq p_1$ $x \geq p_2$

Expected result:

 $p_1 \le 3 \land p_2 \le 3 \land d \in [p_2, 3]$

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- Theory: undecidability
- A practical approach

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Timed-opacity synthesis is (very) difficult

Theorem (Undecidability of timed-opacity-emptiness)

The mere existence of a parameter valuation for which there exists a duration for which timed-opacity is achieved is undecidable.

Proof idea: reduction from reachability-emptiness for PTAs [Alur et al., 1993]



Remark: decidable subclass

(see Theorem 1 in the paper)

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(see Theorem 1 in the paper)

In the following, we adopt a "best-effort" approach

Approach not guaranteed to terminate in theory

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Reducing timed-opacity synthesis to reachability synthesis

Big picture:

- Formalism: parametric timed automata
- Our approach:
 - Perform a (mild) transformation of the PTA
 - 2 Perform self-composition
 - 3 Apply parametric timed model checking (reachability-synthesis)
- Tool support: IMITATOR

[André et al., 2012]



1 Add a Boolean flag b to remember whether ℓ_{priv} was visited



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 m finish}$ on any transition to ℓ_f



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- ${f 2}$ Add a synchronization action ${
 m finish}$ on any transition to ℓ_f
- 3 Measure the (parametric) duration to ℓ_f thanks to a new clock x_{abs} and a new parameter d
- Perform self-composition (i. e., a synchronization on shared actions of the PTA with a copy of itself)



timed model checking



A model of the system

Question: does the model of the system satisfy the property?



PTA for Guaranteeing Timed Opacity

Parametric timed model checking



A model of the system

Question: for what values of the parameters does the model of the system satisfy the property?

Yes if...



 $\begin{array}{l} 2 \text{delay} > \text{period} \\ \wedge \text{period} < 20.46 \end{array}$

Applying reachability-synthesis

We then synthesize all parameter valuations (including d) for which the following discrete state is reachable:

- the original automaton is in ℓ_f with b = true
- the copy automaton is in ℓ_f with b' = false

Applying reachability-synthesis

We then synthesize all parameter valuations (including d) for which the following discrete state is reachable:

- the original automaton is in ℓ_f with b = true
- the copy automaton is in ℓ_f with b' = false

Intuition:

for the same duration (thanks to the synchroniation on finish), we can reach ℓ_f "both" with passing by ℓ_{priv} (i. e., b = true) or without (i. e., b = false)



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Experimental environment

Algorithms

- 1 Timed-opacity: "for a non-parametric TA, is the TA opaque for all execution times?"
- 2 Timed-opacity synthesis: "for a PTA, synthesize parameter valuations and execution times ensuring timed opacity"

Benchmarks

Common PTA benchmarks	
-----------------------	--

- Library of Java programs
 - Manually translated to PTAs
 - User-input variables translated to (non-timing) parameters (supported by IMITATOR)

See experiments at doi.org/10.5281/zenodo.3251141

and imitator.fr/static/ATVA19/

[André, 2019]

https://github.com/Apogee-Research/STAC/

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IMITATOR in a nutshell

- Non-parametric timed-opacity computation
- Parametric timed-opacity synthesis

6 Conclusion and perspectives

IMITATOR

- A tool for modeling and verifying timed concurrent systems with unknown constants modeled with parametric timed automata
 - Communication through (strong) broadcast synchronization
 - Rational-valued shared discrete variables
 - Stopwatches, to model schedulability problems with preemption
- Synthesis algorithms
 - (non-Zeno) parametric model checking (using a subset of TCTL)
 - Language and trace preservation, and robustness analysis
 - Parametric deadlock-freeness checking







IMITATOR

Under continuous development since 2008

A library of benchmarks

- Communication protocols
- Schedulability problems
- Asynchronous circuits
- …and more

Free and open source software: Available under the GNU-GPL license





[André et al., FM'12]

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Try it!

www.imitator.fr

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PTA for Guaranteeing Timed Opacity

[André et al., FM'12]

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Experiments: (non-parametric) timed opacity

Model			Tra	nsf. F	PTA	Result	
Name	$ \mathcal{A} $	X	$ \mathcal{A} $	X	P	Time (s)	Vulnerable?
Fig. 5, [Vasilikos et al., 2018]	1	1	2	3	3	0.02	()
Fig. 1b, [Gardey et al., 2007]	1	1	2	3	1	0.04	()
Fig. 2a, [Gardey et al., 2007]	1	1	2	3	1	0.05	()
Fig. 2b, [Gardey et al., 2007]	1	1	2	3	1	0.02	()
Web privacy problem [Benattar et al., 2015]	1	2	2	4	1	0.07	()
Coffee	1	2	2	5	1	0.05	×
Fischer-HSRV02	3	2	6	5	1	5.83	()
STAC:1:n			2	3	6	0.12	()
STAC:1:v			2	3	6	0.11	
STAC:3:n			2	3	8	0.72	×
STAC:3:v			2	3	8	0.74	()
STAC:4:n			2	3	8	6.40	\checkmark
STAC:4:v			2	3	8	265.52	
STAC:5:n			2	3	6	0.24	×
STAC: 11A: v			2	3	8	47.77	()
STAC: 11B: v			2	3	8	59.35	()
STAC: 12c : v			2	3	8	18.44	\checkmark
STAC: 12e:n			2	3	8	0.58	
STAC: 12e: v			2	3	8	1.10	()
STAC:14:n			2	3	8	22.34	()

imes= not vulnerable; $(\sqrt{})=$ vulnerable, can be repaired; $\sqrt{}=$ vulnerable, cannot be repaired

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Experiments: (parametric) timed-opacity synthesis

Model					ansf. I	PTA	Result	
Name	$ \mathcal{A} $	X	P	$ \mathcal{A} $	X	P	Time (s)	Constraint
Fig. 5, [Vasilikos et al., 2018]	1	1	0	2	3	4	0.02	K
Fig. 1b, [Gardey et al., 2007]	1	1	0	2	3	3	0.03	K
Fig. 2, [Gardey et al., 2007]	1	1	0	2	3	3	0.05	K
Web privacy problem [Benattar et al., 2015]	1	2	2	2	4	3	0.07	K
Coffee	1	2	3	2	5	4	0.10	Т
Fischer-HSRV02	3	2	2	6	5	3	7.53	K
STAC:3:v			2	2	3	9	0.93	K

K= some valuations make the system non-vulnerable; op = all valuations make the system non-vulnerable

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Conclusion

Context: vulnerability by timing-attacks

- Attacker model: observability of the global computation time
- Goal: avoid leaking information on whether some discrete state has been visited

Solution: parametric timed model checking

- Formalism: parametric timed automata
- Our approach:
 - Perform a (mild) transformation of the PTA
 - 2 Perform self-composition
 - 3 Apply parametric timed model checking (reachability-synthesis)
- Toolkit: IMITATOR
- Benchmarks: concurrent systems and Java programs

Perspectives

Theoretical open problems

- Decidability of timed-opacity emptiness remains open for 1 clock
- Case of U-PTAs or L-PTAs

[Bozzelli and La Torre, 2009]

- Automated translation of Java programs
 - Our translation required non-trivial creativity
 - How to automate it?
 - Finer grain needed for "untimed" instructions: probabilistic timings?

Repairing a non-opaque system

- "From PTA parameter tuning back to the original system"
- In programs: using Wait or Sleep
- Preliminary ideas in the paper

- What: Project on quantitative formal methods + security (2020-2023)
- Where: France (Nancy / Nantes), Singapore
- Who: Master students, PhD, post-docs ...starting anytime!

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